



**The Weather
and Climate**

Emergent Laws and Multifractal Cascades

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CAMBRIDGE

Scaling fluctuation analysis and statistical hypothesis testing of anthropogenic warming

GEC3, Nov. 29, 3:30

S. Lovejoy McGill, Montreal

The need for GCM-free approaches to anthropogenic climate change

- Limitations of models: they converge (very slowly!) to *their* climates... not *ours*.
- GCM uncertainties: 1979-2013: 1.5-4.5K, no convergence
- The focus on model issues removes us from real world issues: e.g. the focus on “equilibrium” or “transient” climate sensitivities rather than “effective climate sensitivities”.
- Global warming is only evaluated *indirectly* using models (e.g. “fingerprinting”): the data is not fully exploited.
- The exclusive reliance on GCM’s for assessing anthropogenic warming gives ammunition to climate skeptics.
- The statistical hypothesis that the warming is due to natural variability must be statistically tested. The failure to reject this hypothesis gives ammunition to climate skeptics.

Introduction:

What is Climate?

The climate is not what you expect...

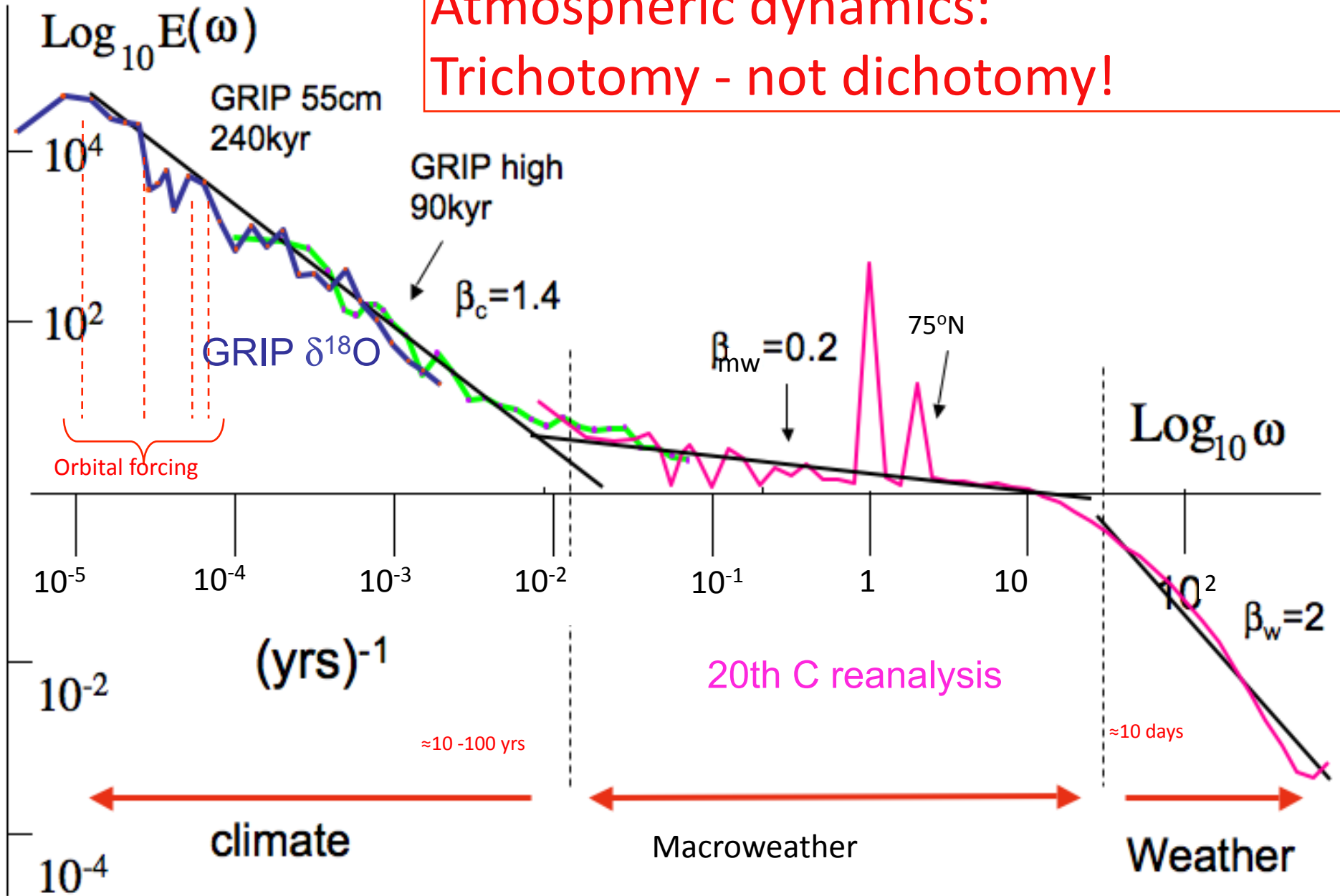
"Climate is what you expect, weather is what you get."

-Lazarus Long, character in R. Heinlein 1973

"Climate in a narrow sense is usually defined as the "average weather" ... The classical period is 30 years, as defined by the World Meteorological Organization (WMO)... Climate in a wider sense is the state, including a statistical description, of the climate system."

-Intergovernmental Panel on Climate Change, 2007

Atmospheric dynamics: Trichotomy - not dichotomy!



Two data sources only GRIP, 20CR

Scaling fluctuation analysis

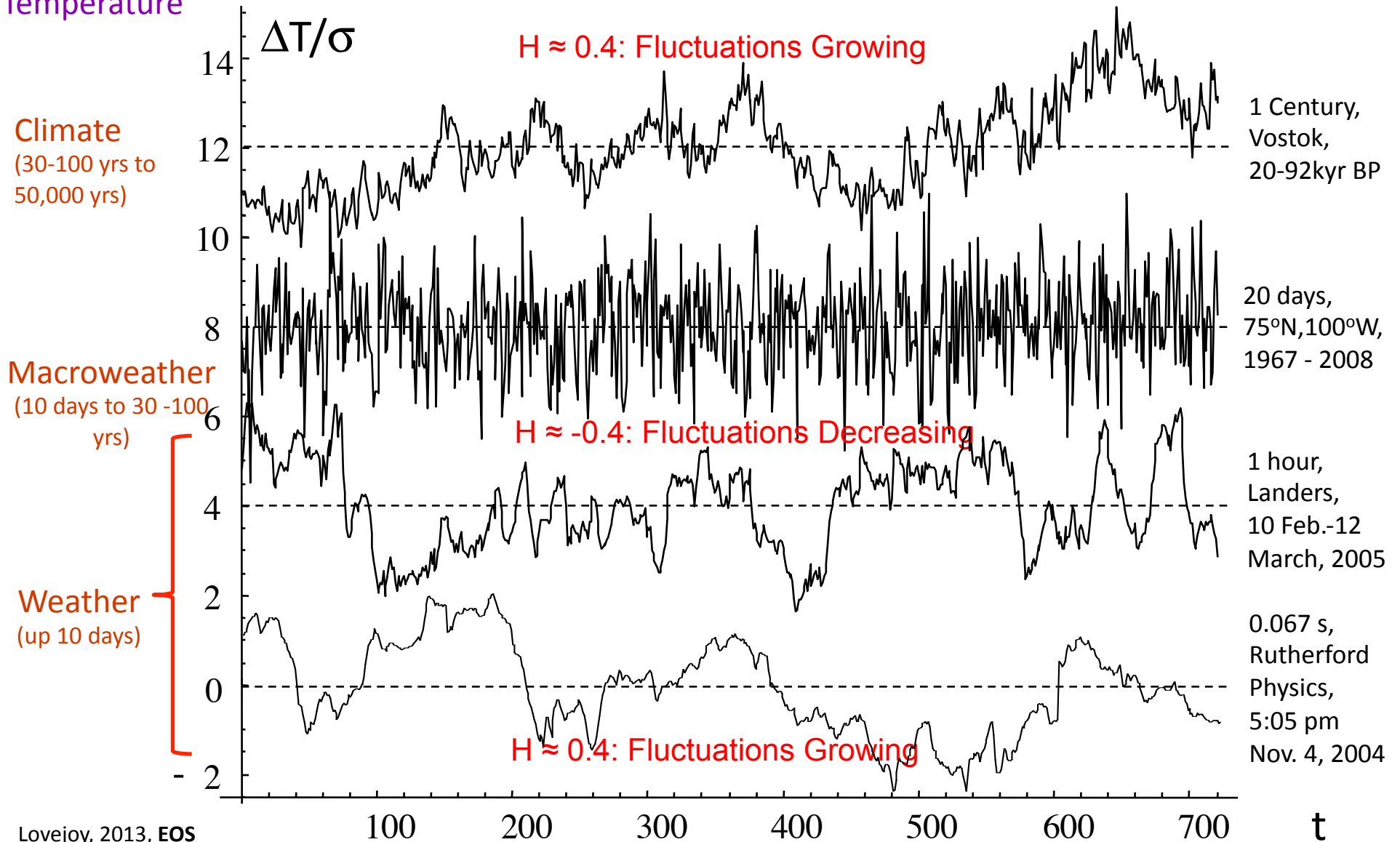
Trichotomy:

Weather – macroweather - climate

$$\langle \Delta I \rangle = \langle \phi \rangle \Delta t^H$$

Fluctuation \rightarrow $\langle \phi \rangle$ \rightarrow constant

Temperature



Basic characteristics of the three regimes

Fluctuation $\rightarrow \langle \Delta I \rangle = \langle \varphi \rangle \Delta t^H$ \rightarrow = constant

"Climate is what you expect, weather is what you get."
-Lazarus Long, character in R. Heinlein 1971

Weather:

$\Delta t < \tau_w$ (≈ 10 days): $H > 0$,

Fluctuations grow with scale "unstable"

"...Weather is what you get"

Macroweather:

(10 days \approx) $\tau_w < \Delta t < \tau_c$ (≈ 10 - 100 yrs): $H < 0$,

Fluctuations diminish with scale;
atmospheric states are "stable".

"Macroweather is what you expect..."

Climate:

(10- 100 yrs \approx) $\tau_c \ll \Delta t \ll 100$ kyrs: $H > 0$,

Fluctuations grow with scale; atmospheric states are "unstable",
subject to "climate change".

"The climate is not what you expect..."

Difference, Tendency, Haar fluctuations

Differences: The difference in temperature between t and $t+\Delta t$

Tendency: The average of the temperature (with overall mean removed) between t and $t+\Delta t$

Haar: The difference between the average of the temperature from t and $t+\Delta t/2$ and from $t+\Delta t/2$ and $t+\Delta t$

Relations: When $1 > H > 0$: Haar \approx difference
When $0 > H > -1$: Haar \approx tendency

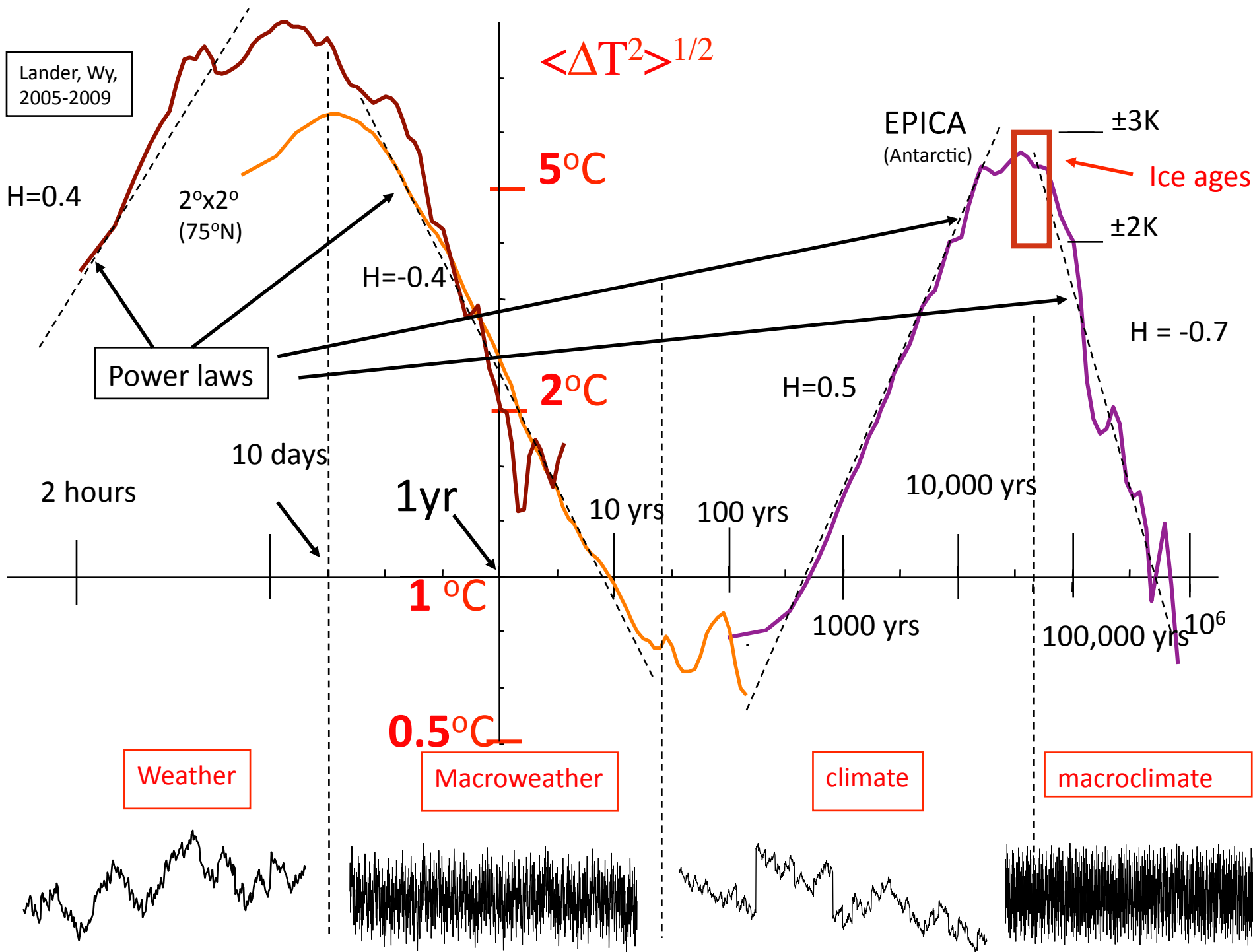


Figure illustrating the multi-scale behavior of temperature fluctuations. The plot shows the standard deviation of temperature fluctuations, $\langle \Delta T^2 \rangle^{1/2}$, versus time scale. The data is divided into four regimes: Weather (2 hours to 10 days), Macroweather (10 days to 10 years), climate (10 years to 10,000 years), and macroclimate (10,000 years to 10⁶ years). The power-law slopes are H=0.4 for Weather, H=-0.4 for Macroweather, H=0.5 for climate, and H=-0.7 for macroclimate. The plot also shows data from Lander, Wyoming (2005-2009) and EPICA (Antarctic). The temperature fluctuations are shown to be self-similar across scales, with a characteristic temperature change of 5°C at 10 days, 2°C at 1 year, and 1°C at 10 years. The macroclimate regime shows large-scale fluctuations, including ice ages, with a range of ±3K and ±2K.

Range of exponents over which average fluctuations at scale Δt corresponds to frequency $1/\Delta t$

Fluctuation $\langle \Delta I \rangle = \langle \varphi \rangle \Delta t^H = \text{constant}$

$$E(\omega) = \langle |\tilde{I}(\omega)|^2 \rangle = \omega^{-\beta}$$

$$\beta = 1 + 2H - K(2)$$

Statistic	Range of H	Range of β	Comment
Spectrum	$-\infty < H < \infty$	$-\infty < \beta < \infty$	$E(\omega) \approx \omega^{-\beta}$
Difference	$0 < H < 1$	$1 < \beta + K(2) < 3$	"Poor man's wavelet"
Tendency Fluctuation	$-1 < H < 0$	$-1 < \beta + K(2) < 1$	Average with overall mean removed (standard deviation= "Climactogram", also called the "Aggregated Standard Deviation")
Haar	$-1 < H < 1$	$-1 < \beta + K(2) < 3$	Difference of means of first and second halves of interval
Detrended Fluctuation Analysis (DFA, polynomial order n)	$-1 < H < (n+1)$	$-1 < \beta + K(2) < 3+2n$	Also multifractal extension (MFDFA), usually linear: n=1, Not a wavelet
Mexican Hat Wavelet	$-1 < H < 2$	$-1 < \beta + K(2) < 5$	2 nd Derivative of a Gaussian
Generalized Haar	$-m < H < n$	$1-2m < \beta + K(2) < 3+2n$	Simple implementation, Interpretation not simple

Multifractal "correction"

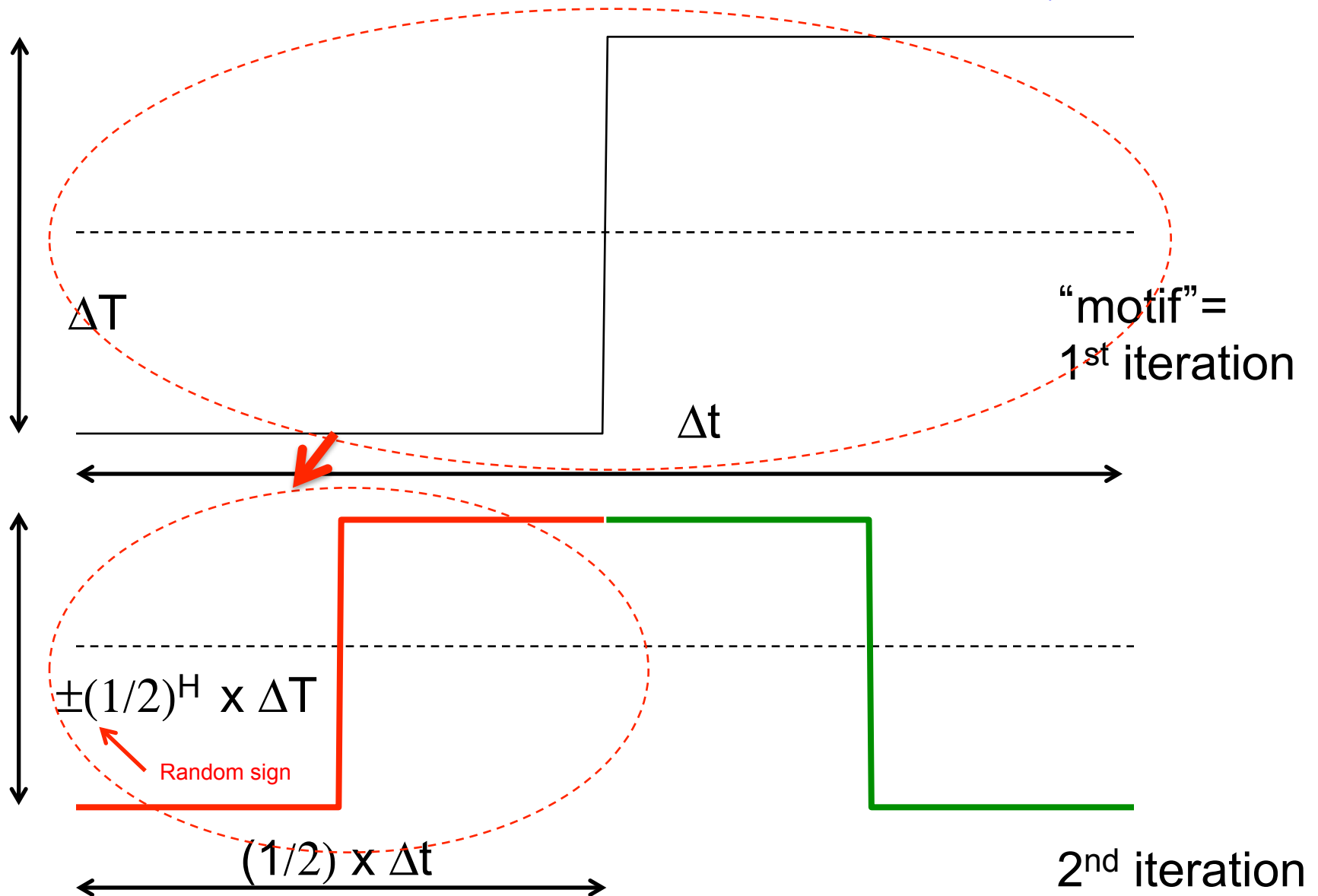
Simple interpretation

To understand the different regimes

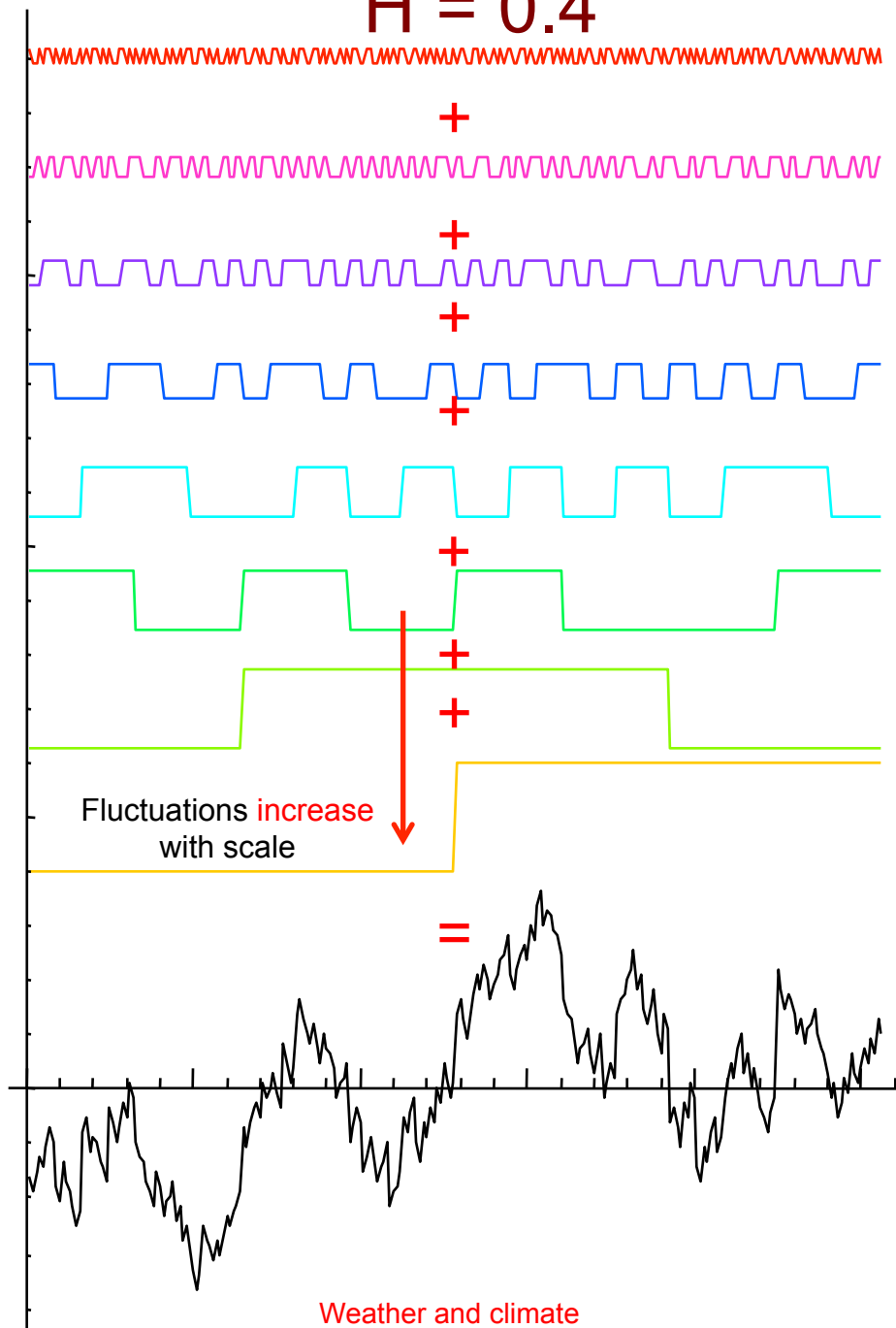
The fractal H model

(Lovejoy 2013)

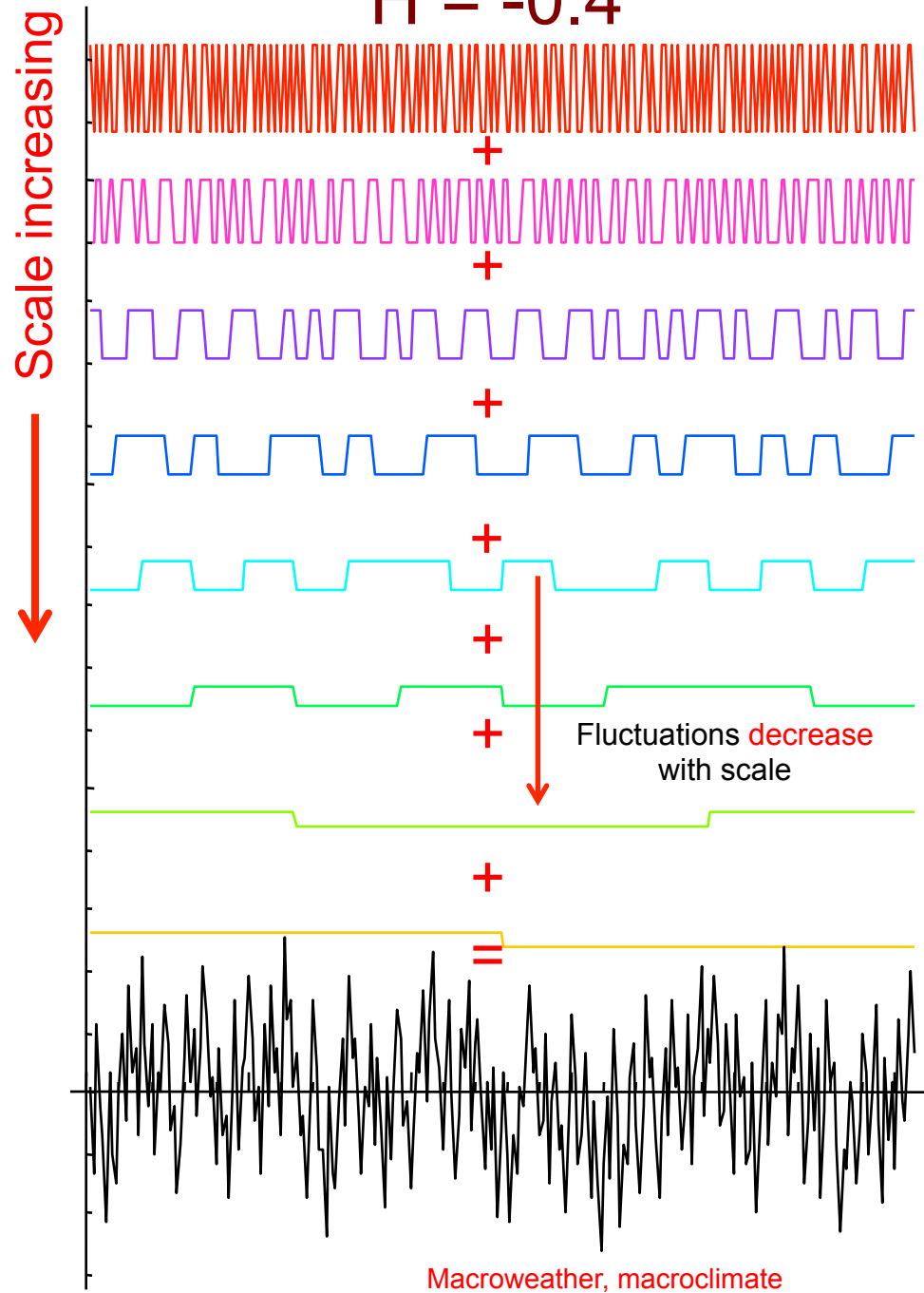
(fractal dimension = $2-H$)



$H = 0.4$



$H = -0.4$



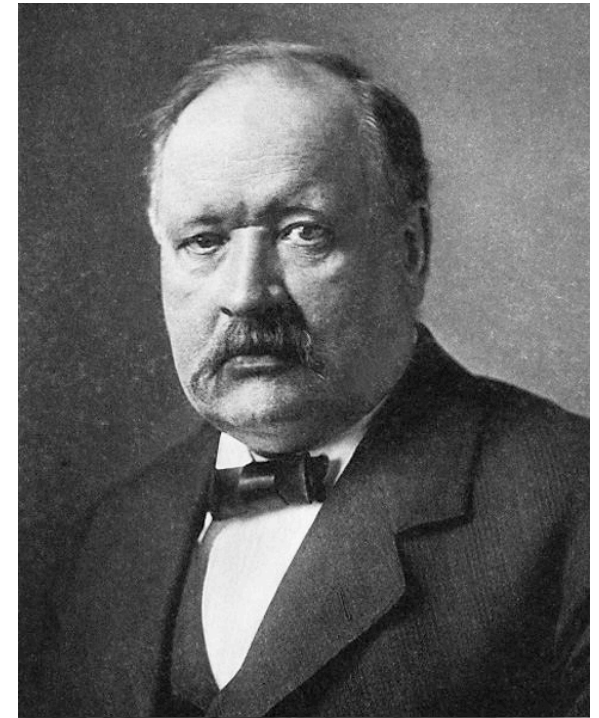
Anthropogenic warming due to
Greenhouse gases: origins and
limitations of GCM approaches

Father of climate sensitivity estimates

Svante Arrhenius

(1859 –1927)

In 1896 predicted CO₂ doubling would increase the earth's temperature by 5-6°C

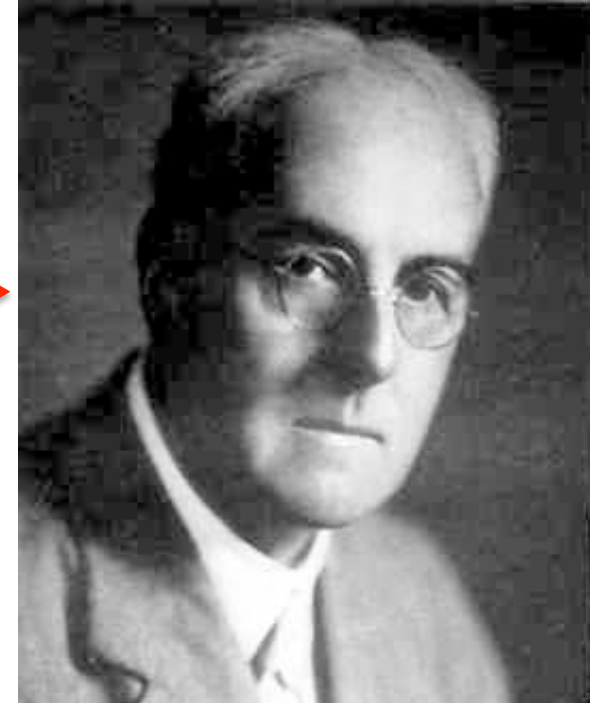


Father of numerical models of the atmosphere

Lewis F. Richardson

(1881-1953)

In 1920, first numerical integration of equations (10⁻² Flops (?)) →



3,120,000
cores: 3x10¹⁶
Flops →



MilkyWay-2: World's fastest supercomputer (June 2013)
National University of Defense Technology, Changsha, China

GCM's uncertainties: no convergence

Evolution of estimates of sensitivity to CO₂ doubling

Date	1896	1979	1990	1995	2002	2007	2013	2013
Source	Arrhenius	US Acad. Sci.	IPCC AR1	IPCC AR2	IPCC AR3	IPCC AR4	IPCC AR5	This study
Sensitivity	5 -6	1.5 -4.5	1.5 -4.5	1.5 -4.5	1.5 -4.5	2 -4.5	1.5 -4.5	1.94 -4.24

↑
Uncertainty due to
water vapour feedbacks

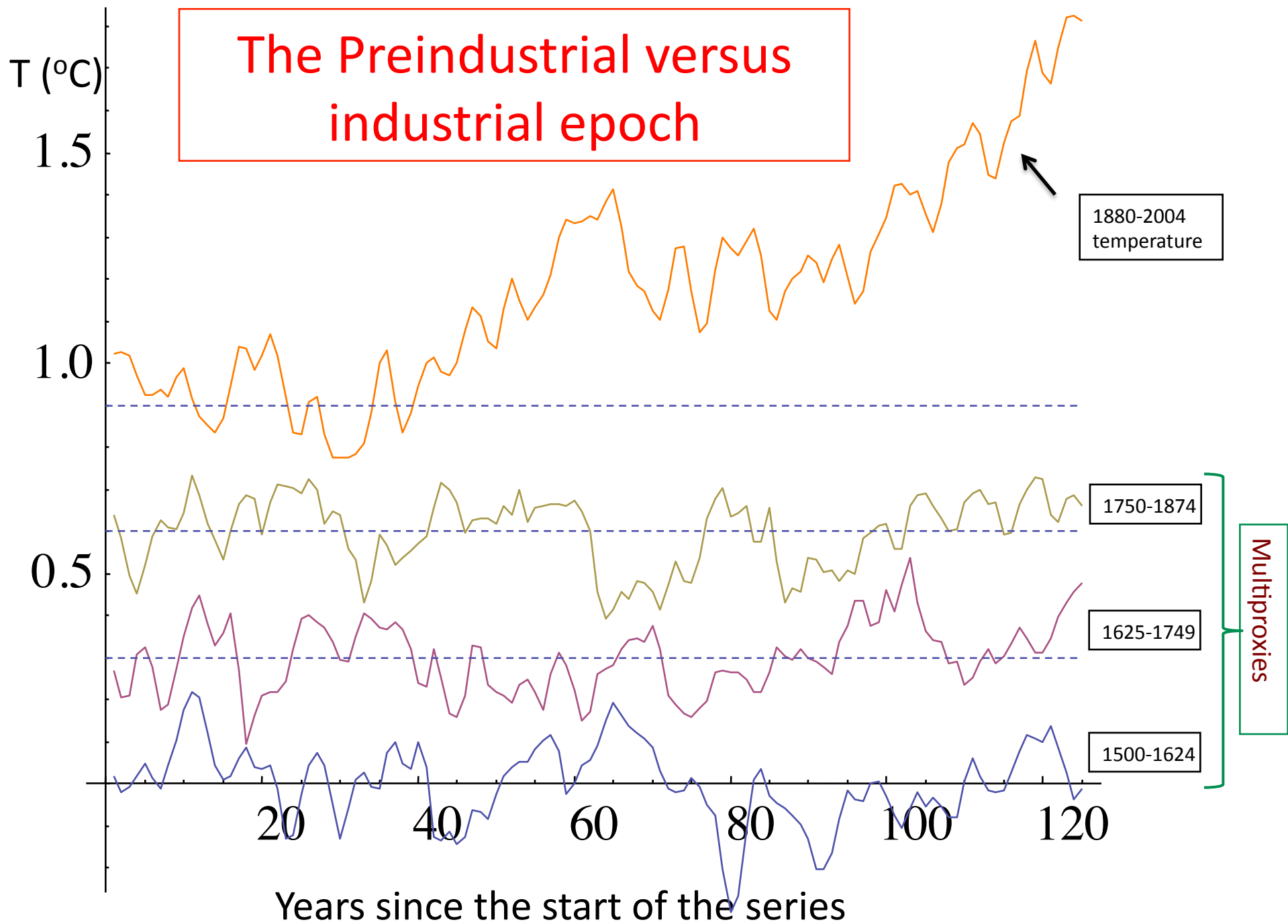
GCM's: Uncertainty due to water vapour, clouds and aerosols

↑
Uncertainty due to
ocean- atmosphere lag

“...due to profound uncertainties, primarily with the hydrological cycle, we are still unable to rule out the possibility that anthropogenic climate change will be catastrophic for humanity over the coming century, or something to which we can adapt relatively easily...”

-Tim Palmer, president of the Royal Meteorological Society, 2012

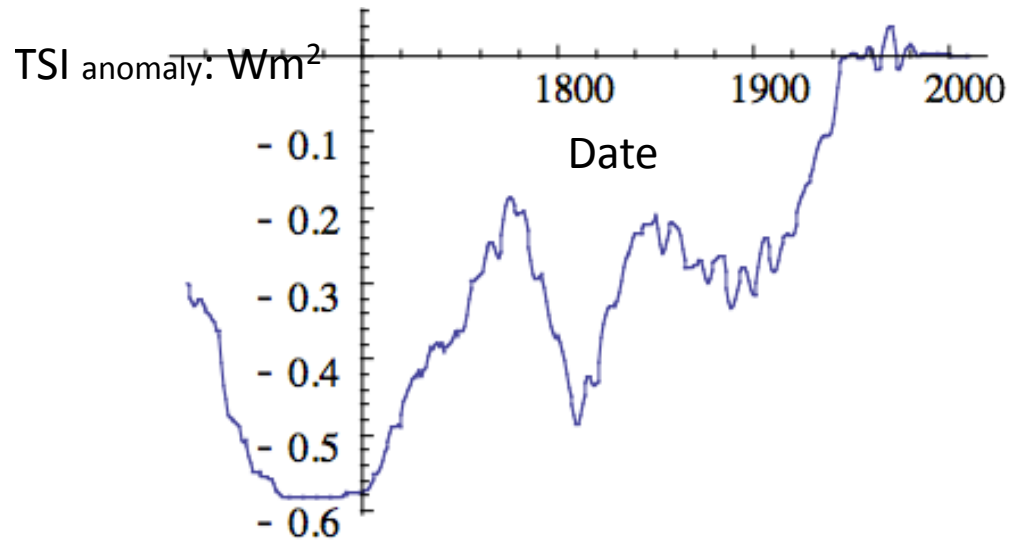
Primary evidence for anthropogenic warming



Warming: don't blame the sun or
volcanoes!

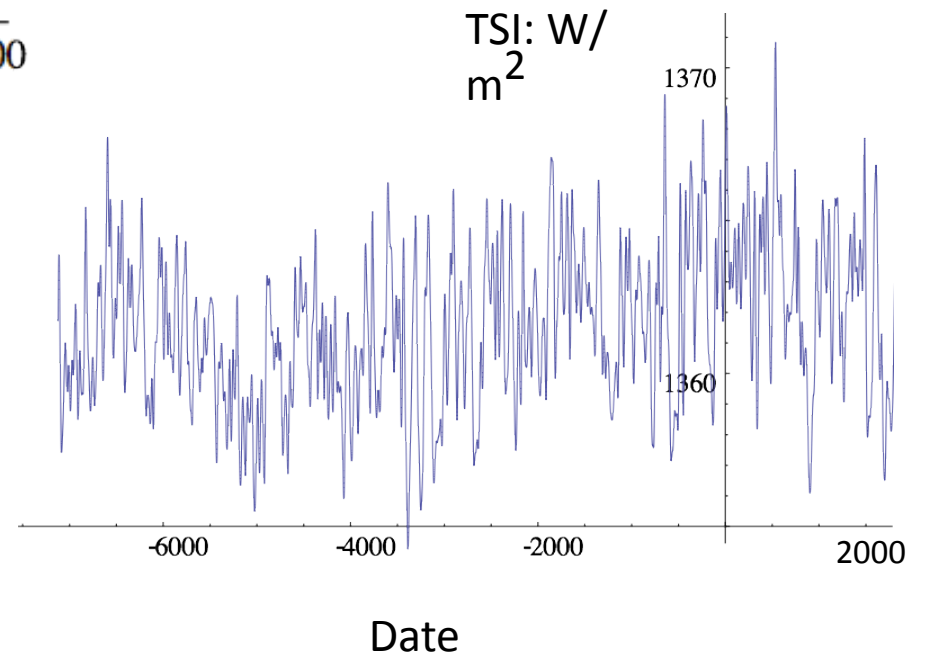
Solar forcing

Sunspot derived “background”
(Wang et al 2005)



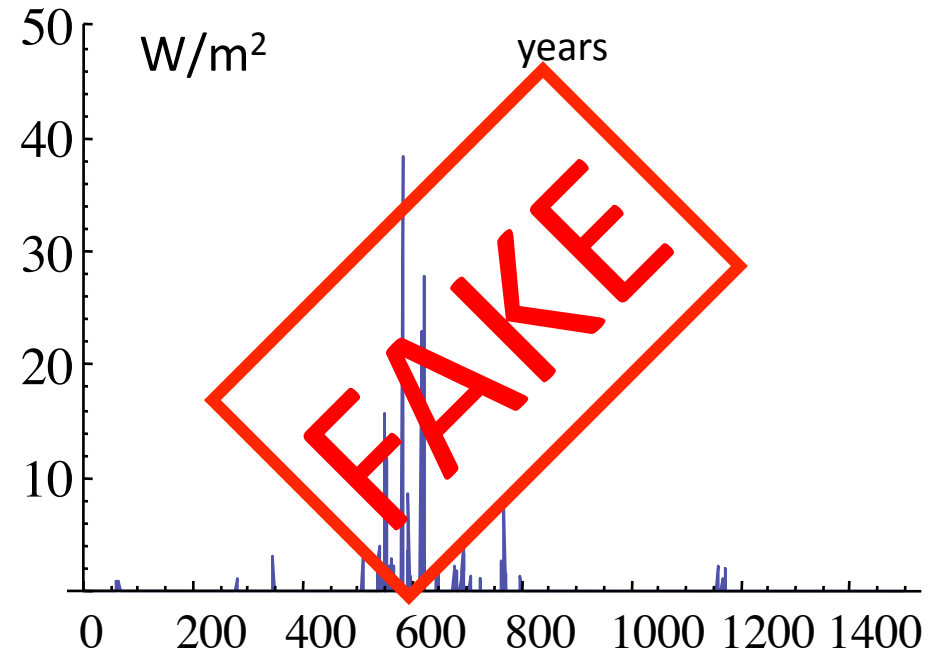
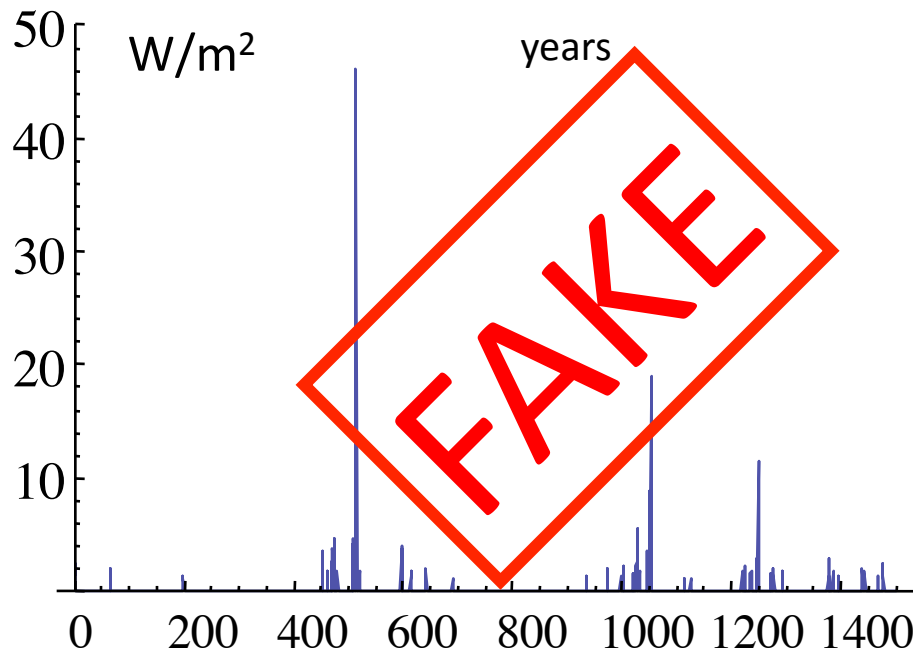
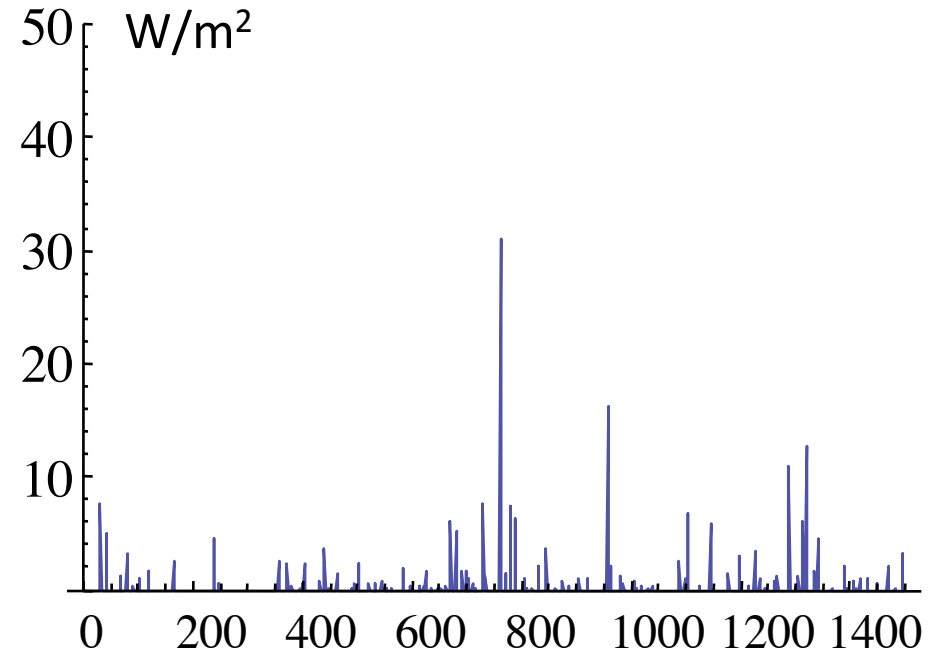
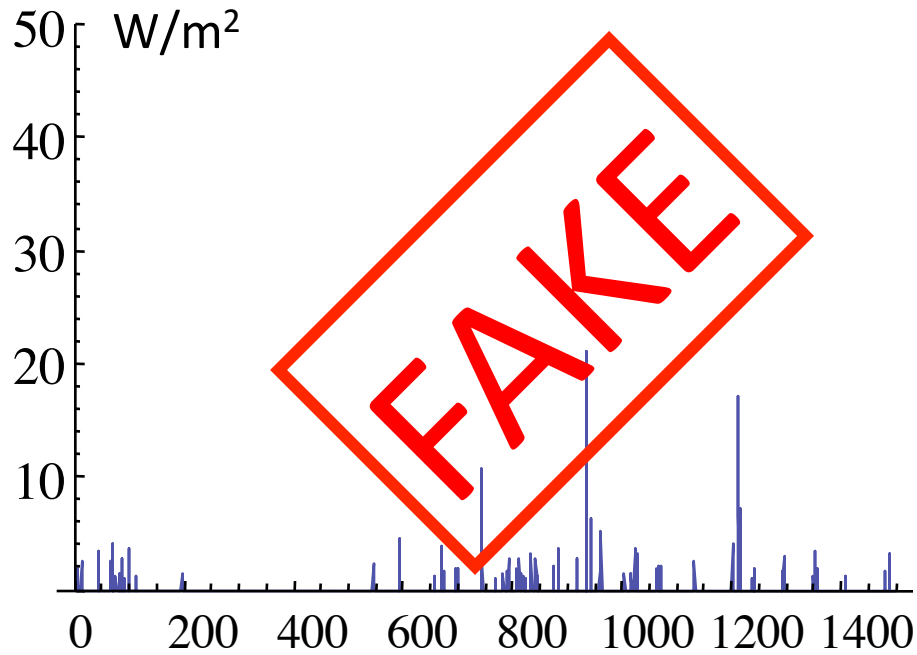
$H \approx +0.4$

^{10}Be solar reconstruction
(Shapiro et al 2011)

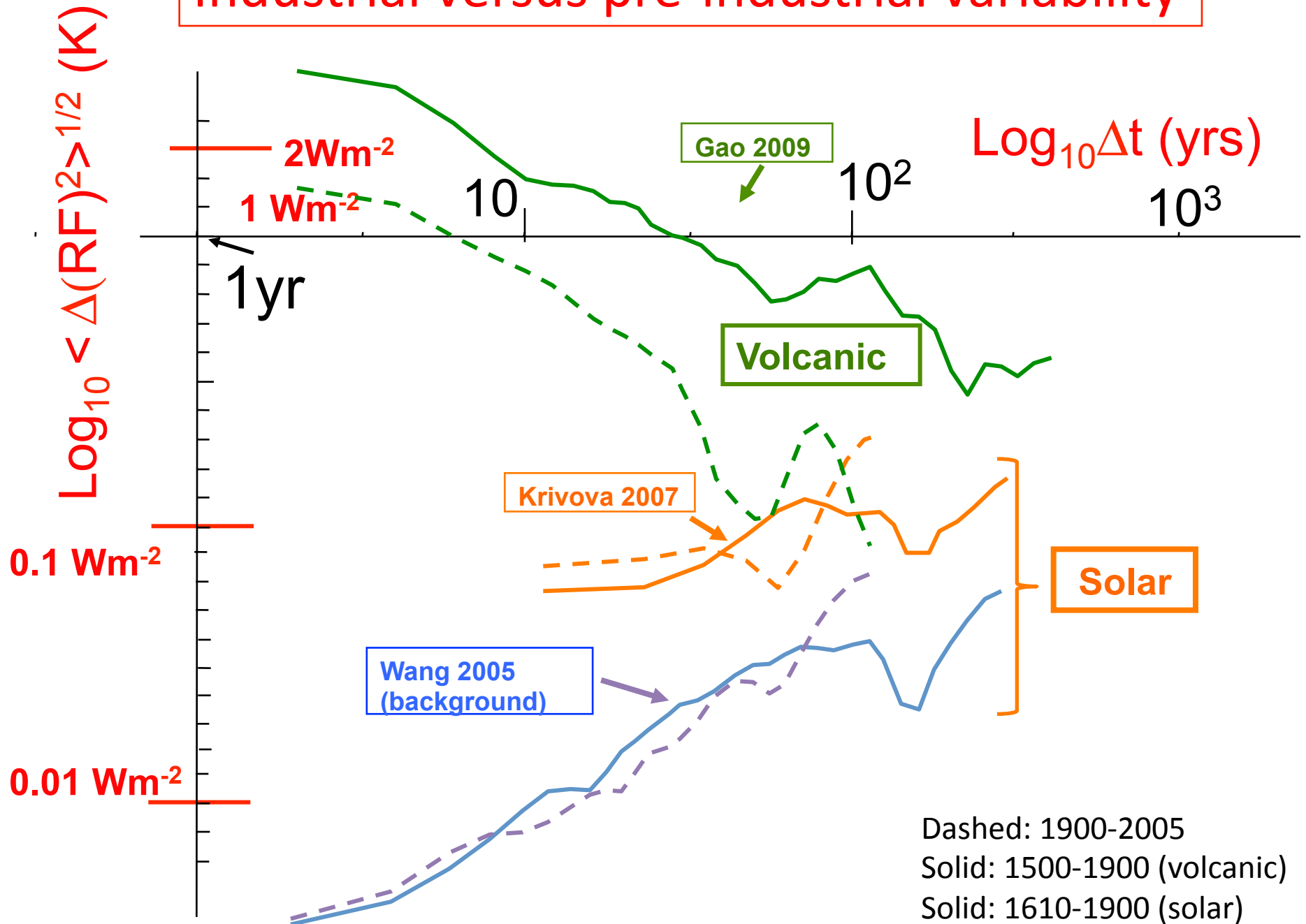


$H \approx -0.4$

Volcanic forcings over last 1500 years are multifractal (intermittent), yet statistically stationary

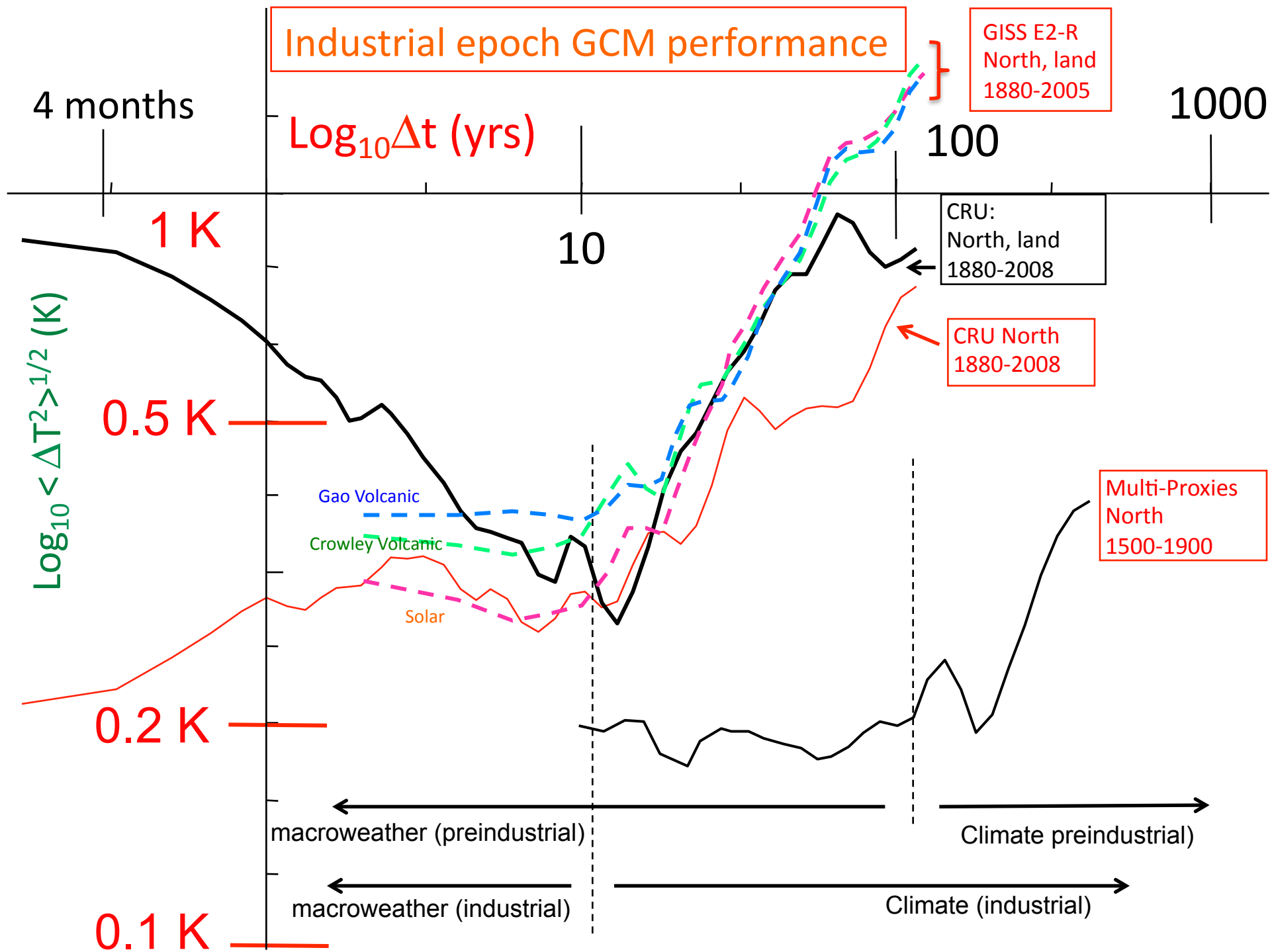


Industrial versus pre-industrial variability

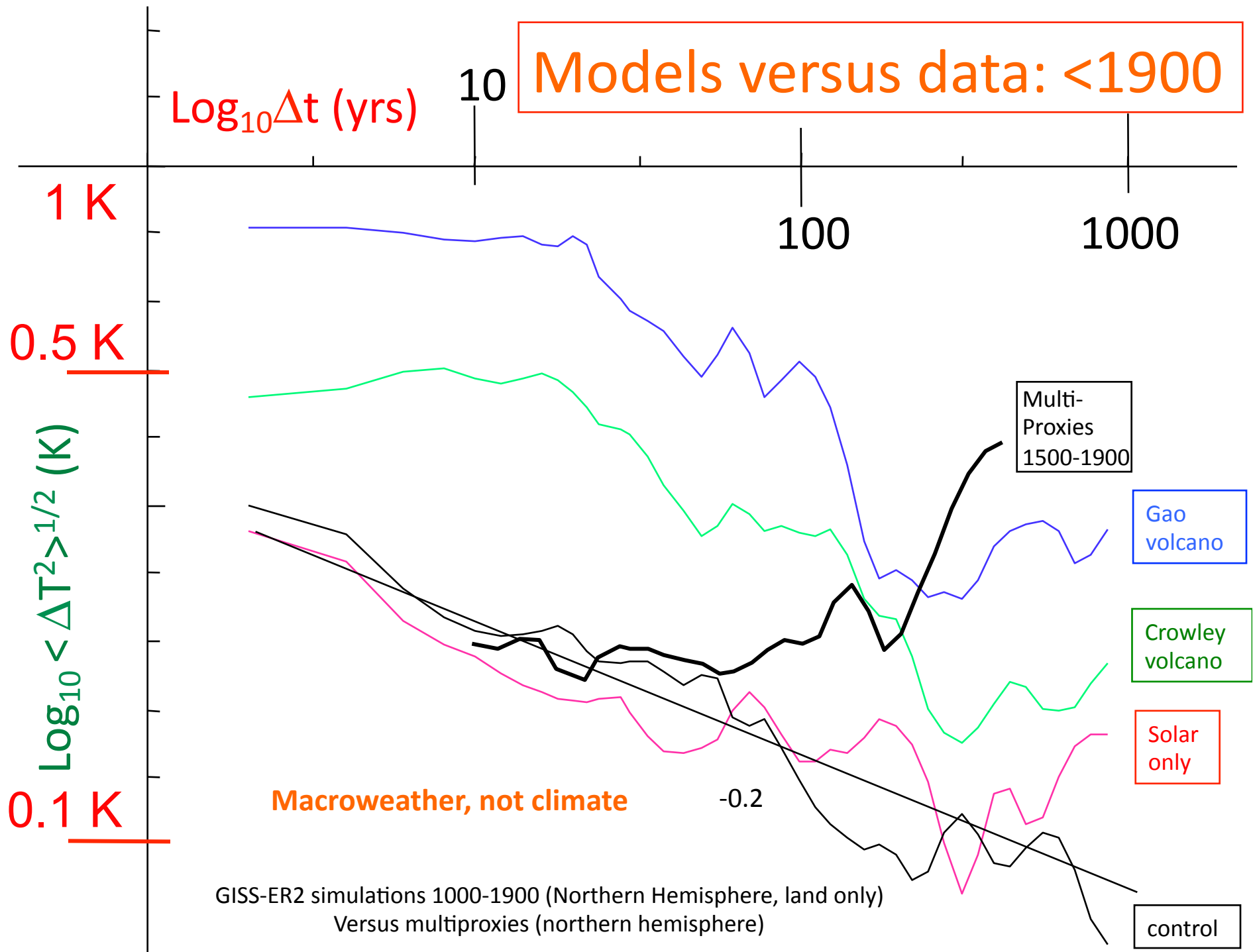


How well do the GCM's do?

Performance quantified by scaling
fluctuation analysis



Models versus data: <1900



Converge of GCM's:

Their climate v.s. our climate

$\text{Log}_{10} S \text{ (K)}$

4000 km: 36°

GISS-20CR (raw)

180°

Red
(GISS-20CR
anomaly)
shifted up
+0.3

4 K

GISS-20CR (anomaly)

0.4

1 $\approx \pm 2\text{K}$

2

4

8

$\approx \pm 1\text{K}$

0.5

2 K

Brown
(GISS-GISS)
shifted up

1

2

4

8

16

$\text{Log}_{10} \Delta\theta$

1.0

1.5

2.0

32

64

128

256

512

0.5 K

-0.5

0.2 K

-1.0

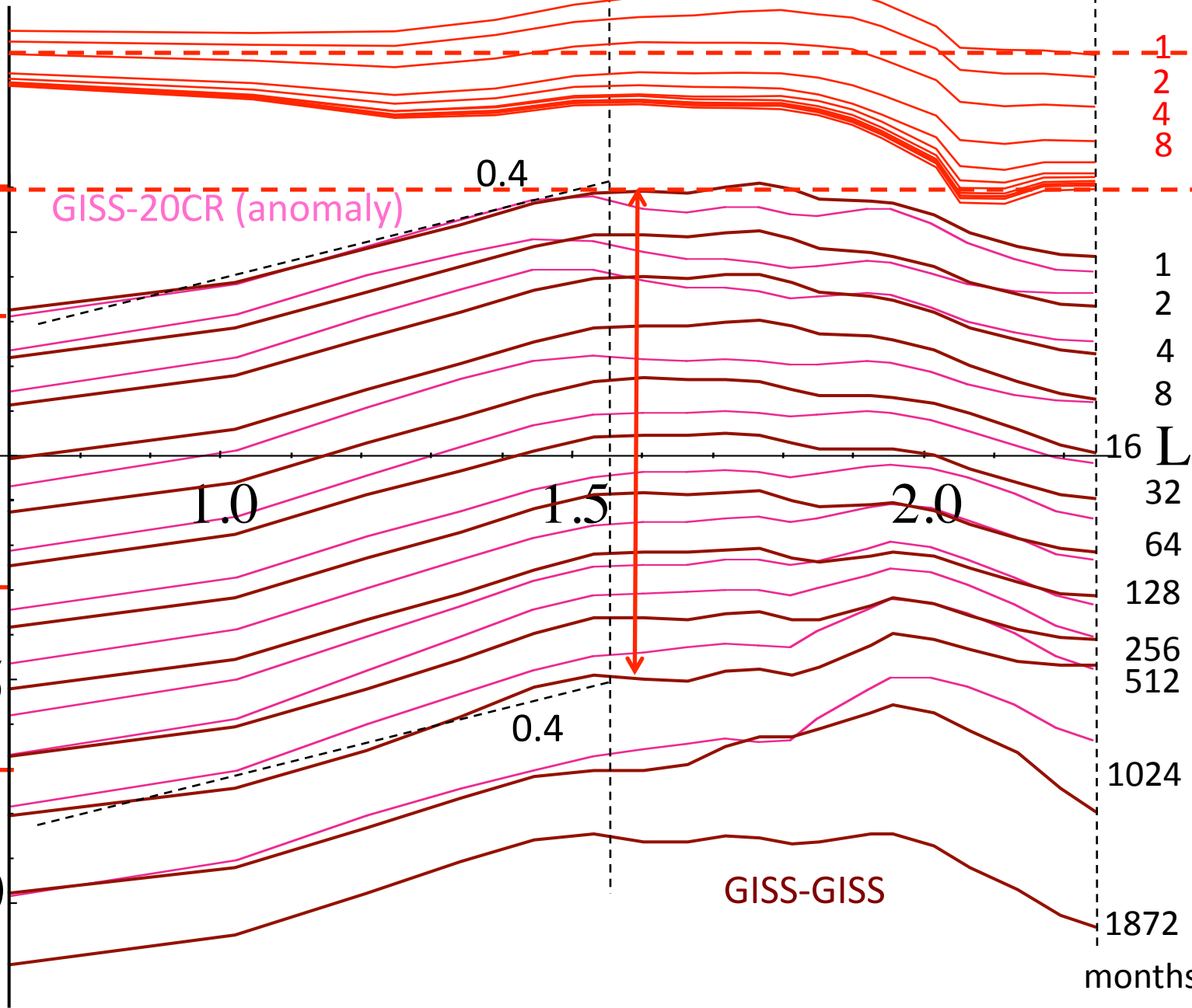
0.4

1024

GISS-GISS

1872

months



GCM-free quantification of Anthropogenic effects (including extremes)*

Premise: if anthropogenic warming is as strong as claimed, then
why do we need huge numerical models to demonstrate it?

*Thanks to the Quebec Skeptical Society!

Two simple theoretical innovations

1. Deterministic Anthropogenic $T_{anth}(t)$

Stochastic natural variability $T_{nat}(t)$ ←

Statistically stationary

responses to both volcanic, solar and any other natural forcings ≠ pure “internal” variability

2. Use of CO₂ radiative forcing as a linear surrogate of all anthropogenic forcings (justified by economic activity).

Climate in the recent epoch: Natural variability and anthropogenic change

$$T_{globe}(t) = T_{anth}(t) + \Delta T_{natural}(t) + \epsilon(t)$$

Anthropogenic contribution
(deterministic)

Small fluctuations due to natural variability
(stochastic)
Includes responses to solar, volcanic and other natural forcings

Measurement error: $\approx \pm 0.03K$

Anthropogenic concentration proportional to the CO₂ radiative forcing

$$T_{anth}(t) = \lambda_{CO_2,eff} R_{F,CO_2}$$

The climate sensitivity (K/(W/m²))

CO₂ radiative forcing (W/m²)

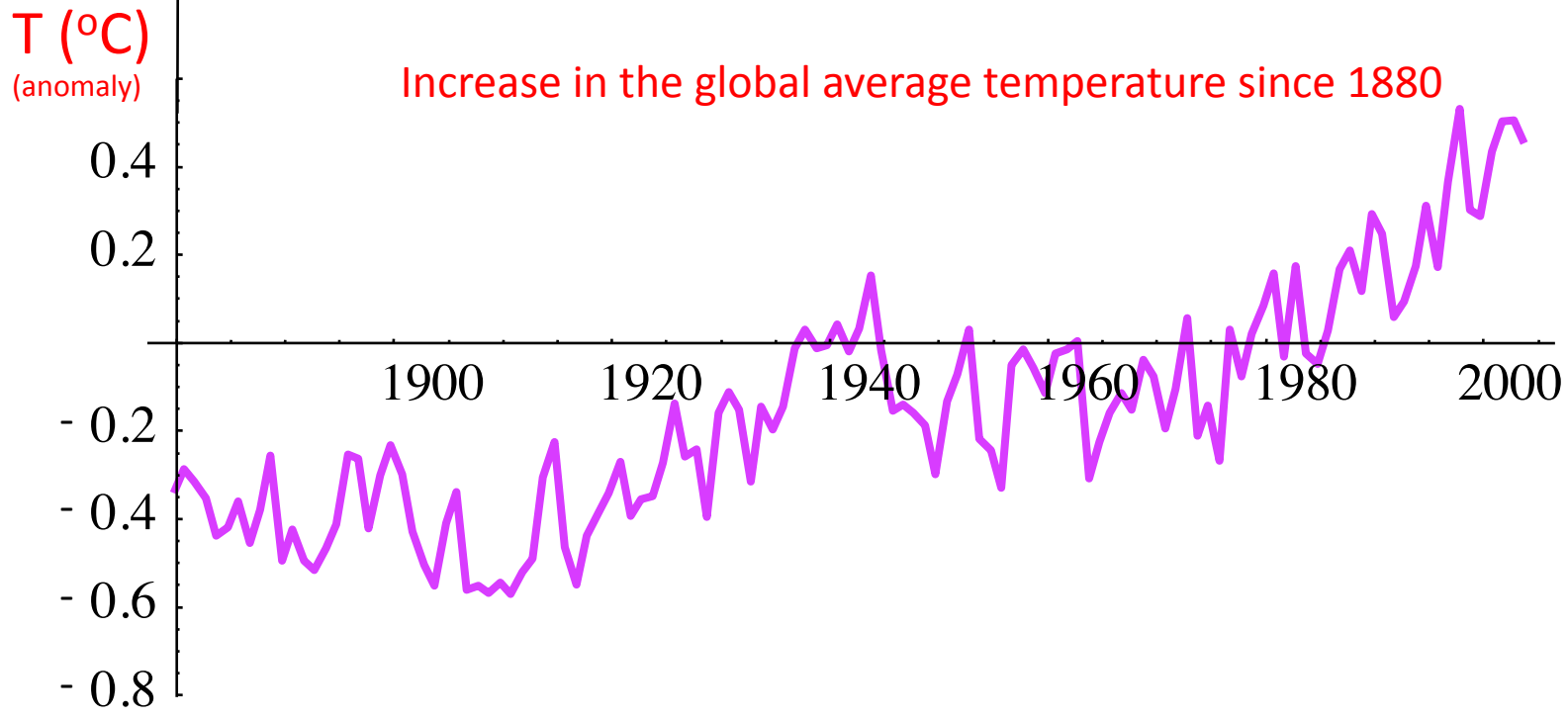
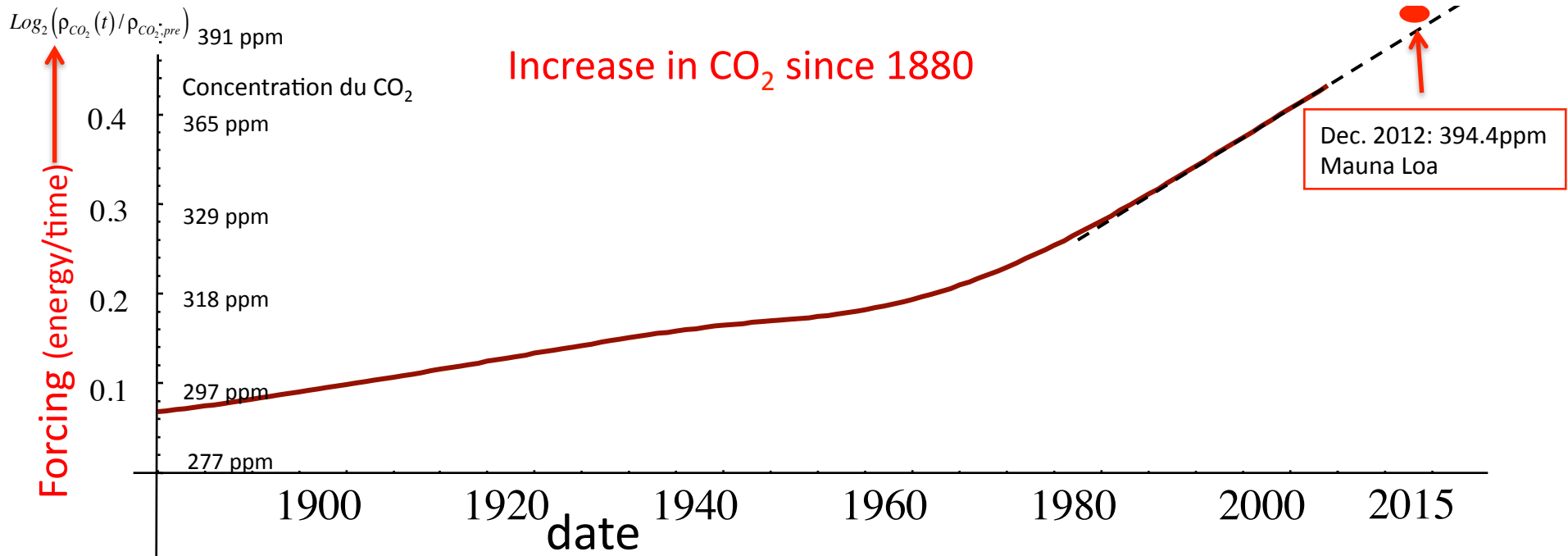
Standard relation for CO₂ radiative forcing

$$R_{F,CO_2} = R_{F,2xCO_2} \log(\rho_{CO_2} / \rho_{CO_2,pre}); \quad R_{F,2xCO_2} = 3.7W / m^2; \quad \rho_{CO_2,pre} = 277 ppm$$

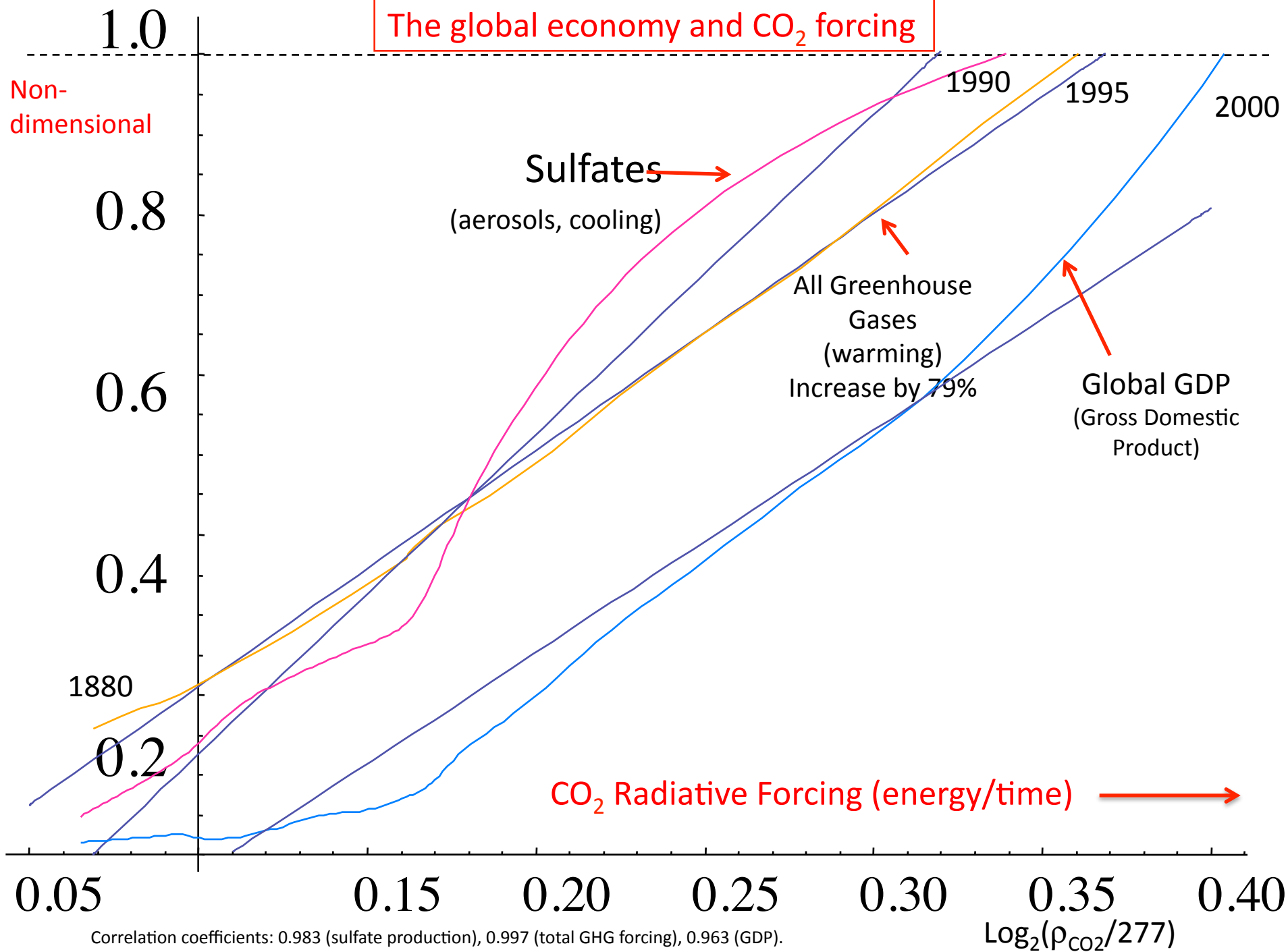
CO₂ concentration

Pre-industrial concentration

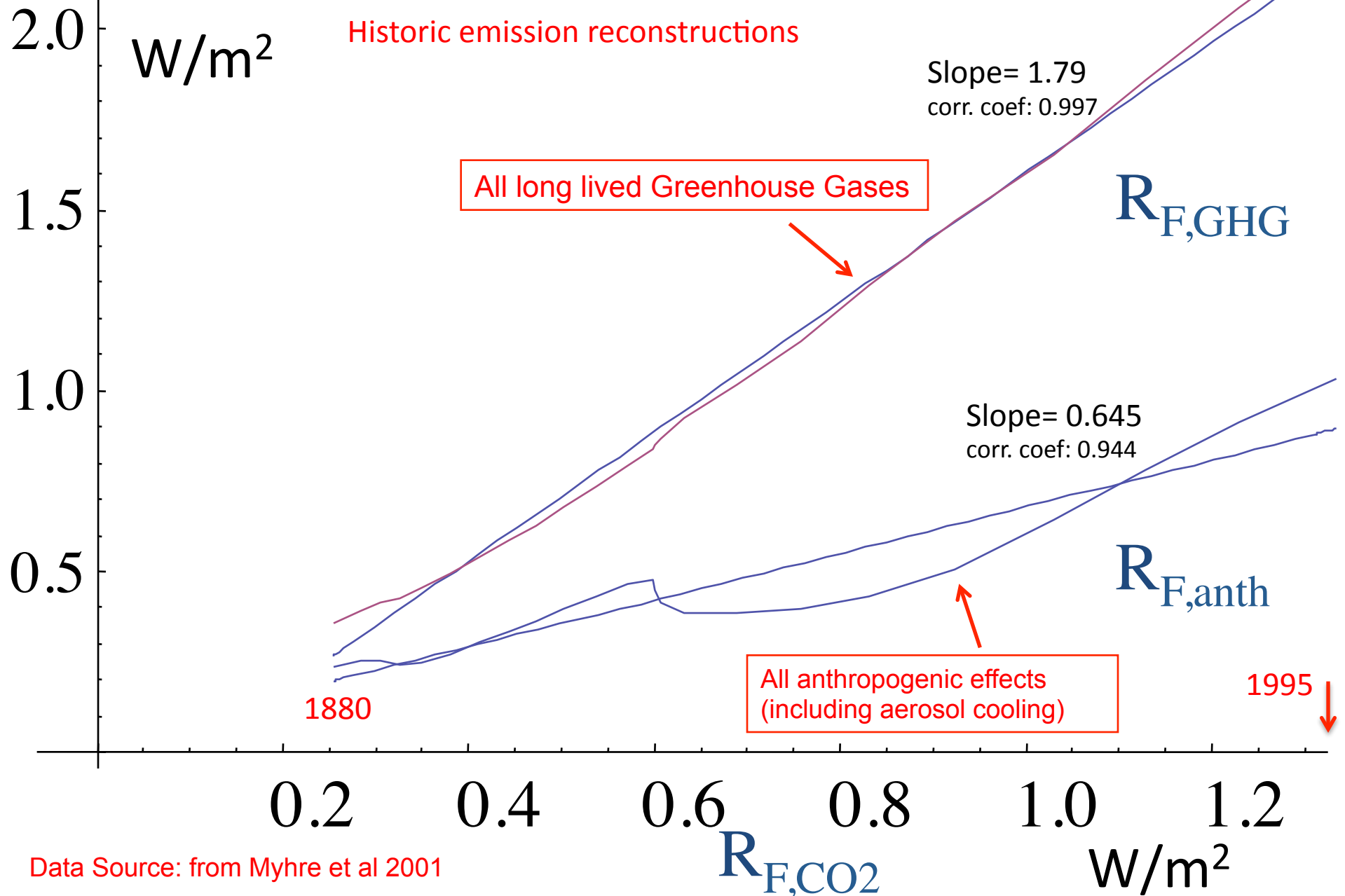
Radiative forcing of CO₂ doubling



The global economy and CO₂ forcing



CO₂ as a surrogate for all anthropogenic effects



Data Source: from Myhre et al 2001

Natural variability as a perturbation to anthropogenic change

$$T_{globe}(t) = \lambda_{2xCO_2,eff} \underbrace{\log_2(\rho_{CO_2}(t) / \rho_{CO_2,pre})}_{\substack{\text{Proportional to CO}_2 \\ \text{radiative forcing (W/m}^2\text{)}}} + \Delta T_{natural}$$

Effective climate sensitivity (K/(W/m²))

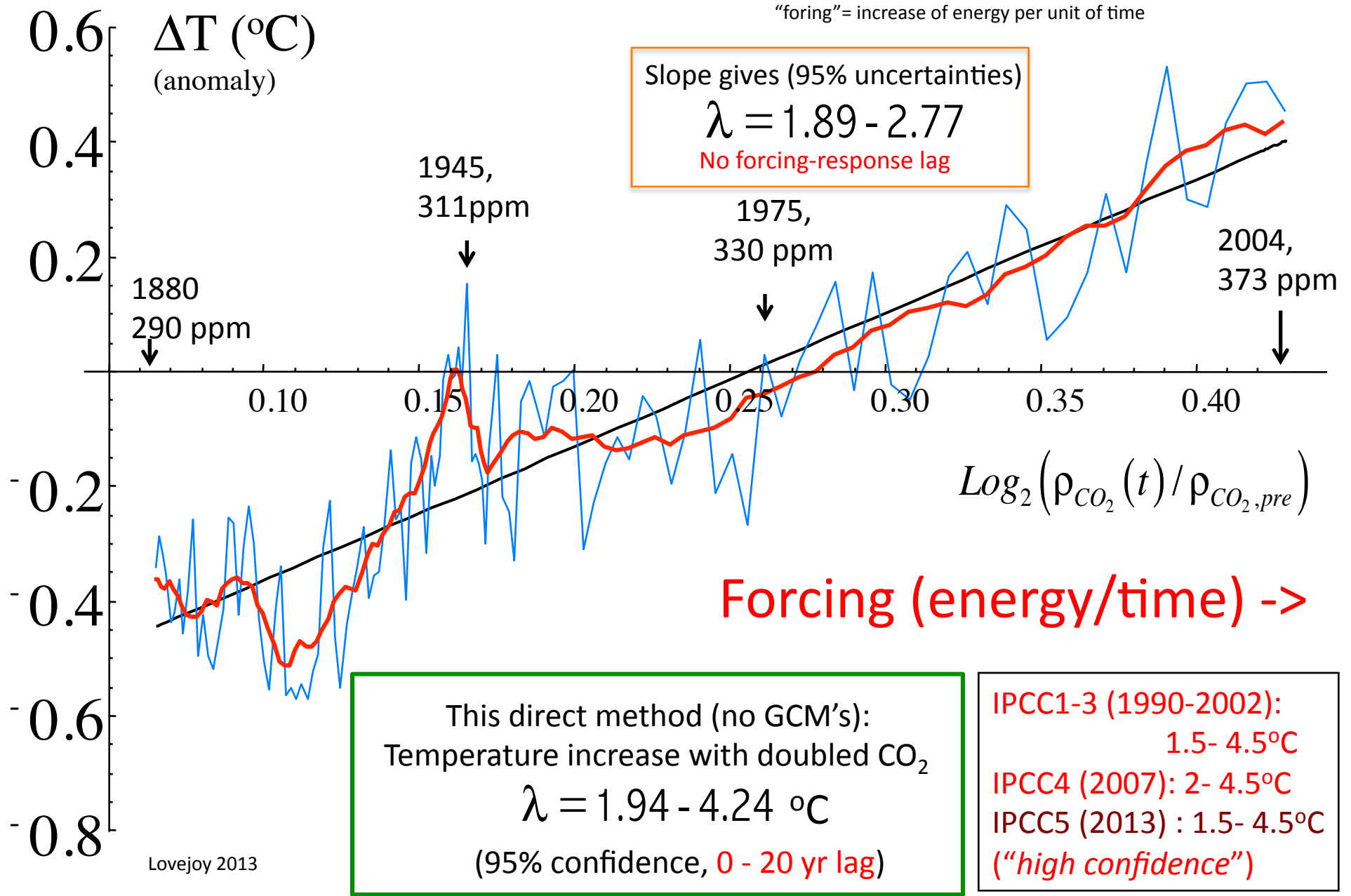
Linear **Surrogate** for all anthropogenic forcings (deterministic)

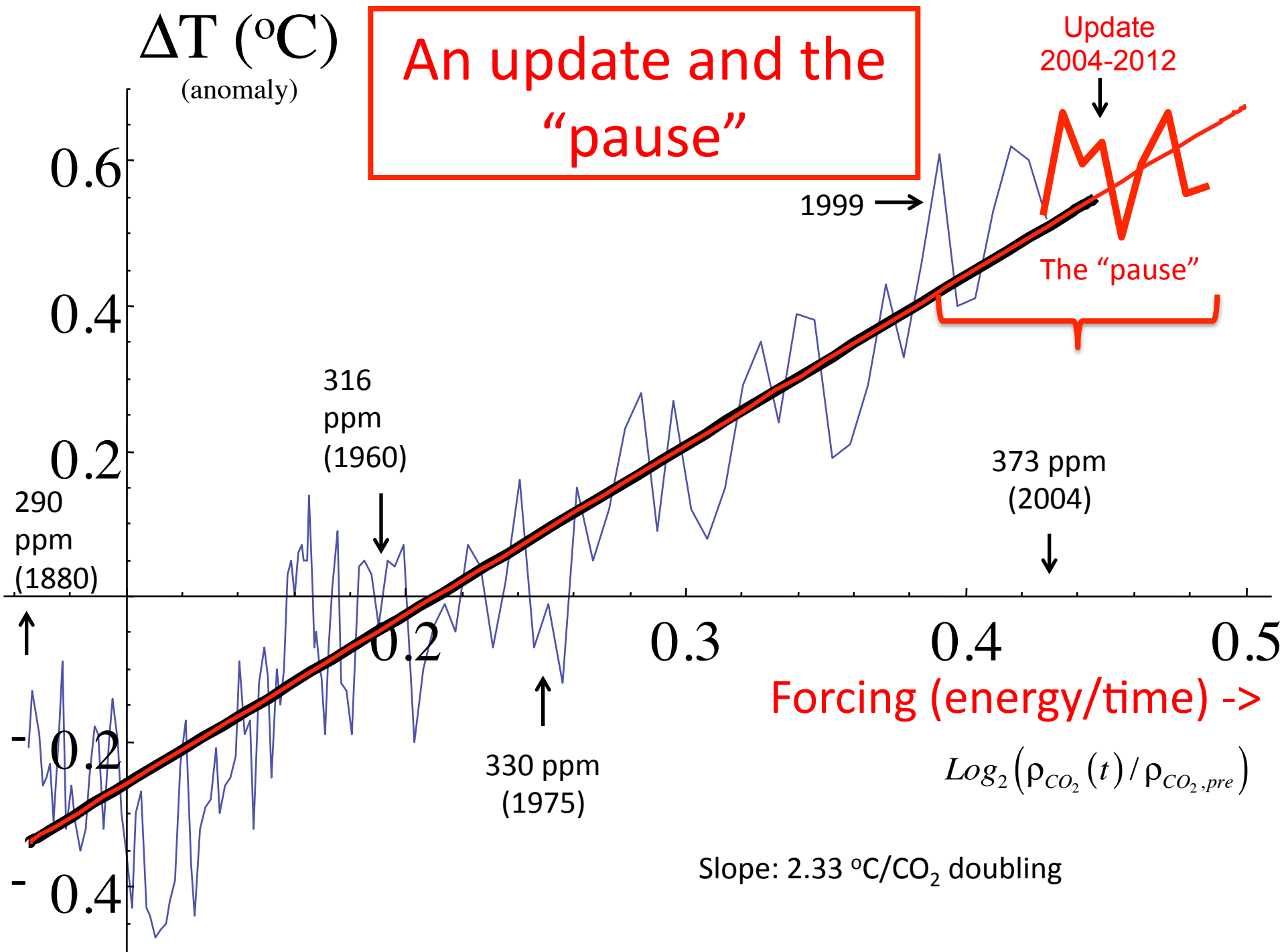
Small fluctuations due to natural variability (stochastic).
Includes responses to solar, volcanic and other natural forcings.

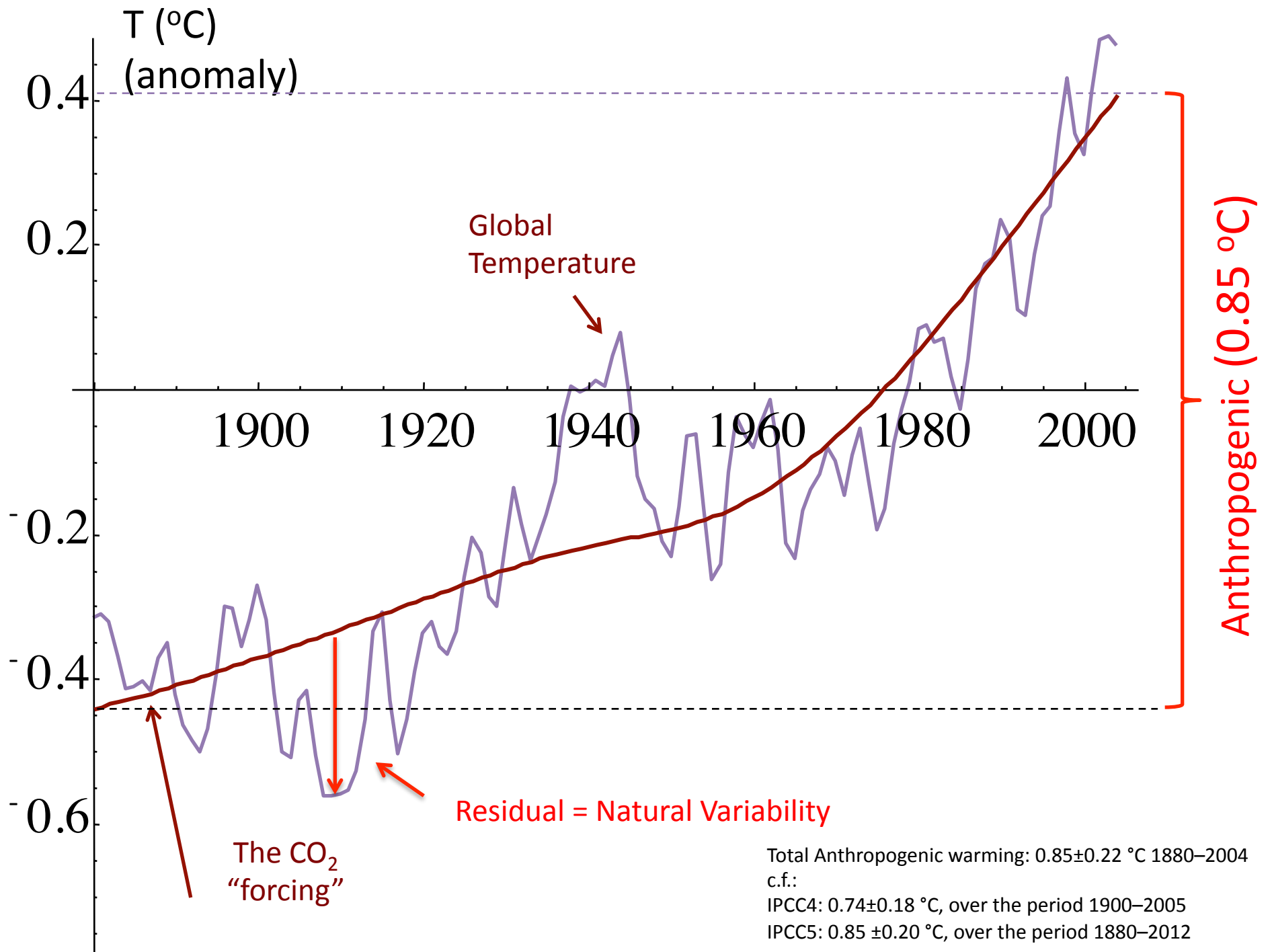
Justified if:

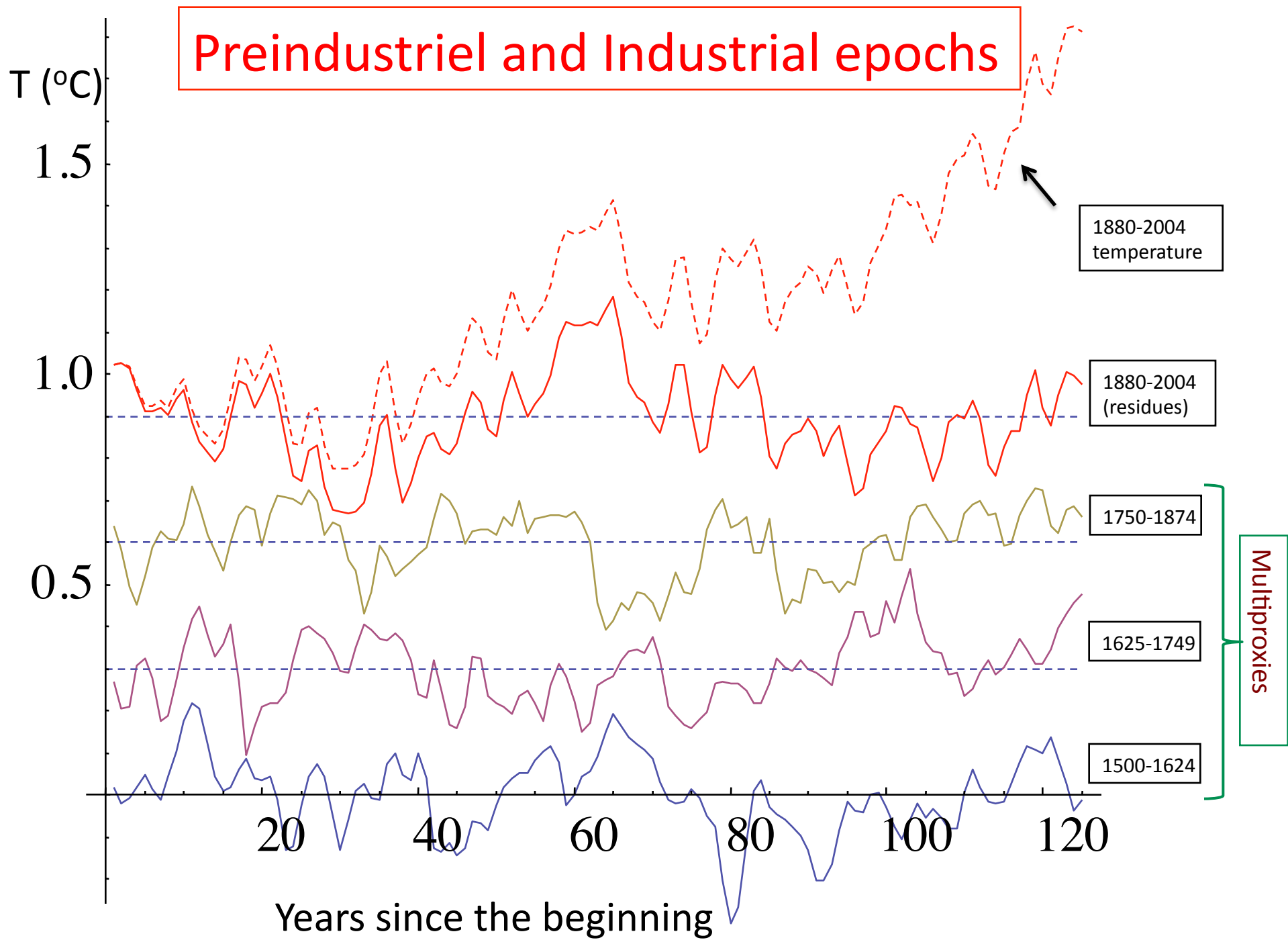
- the anthropogenic effects do not effect the *type* of internal dynamic (variability),
- nor their responses to (natural) external forcing

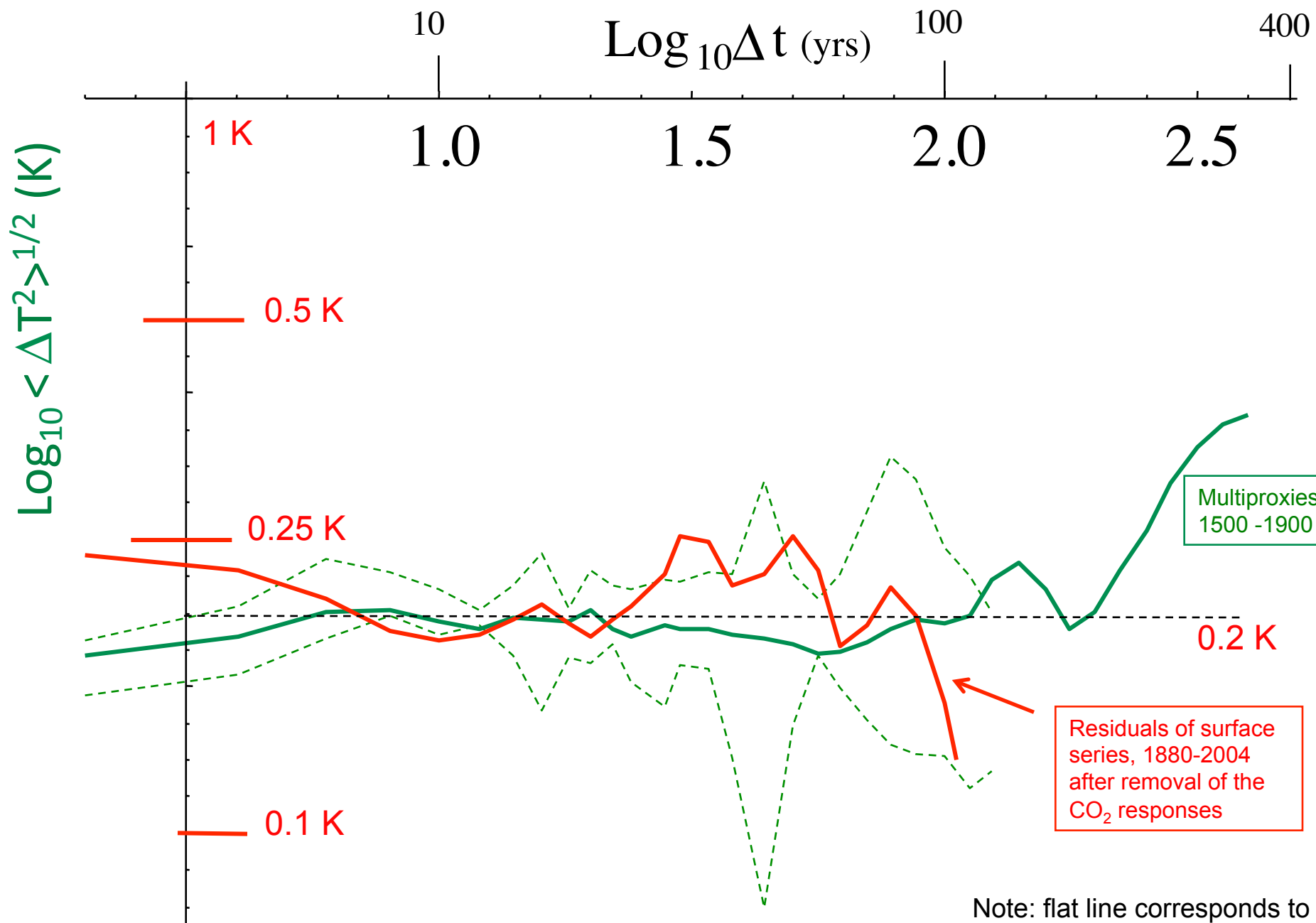
The Temperature is nearly linear with the CO₂ forcing











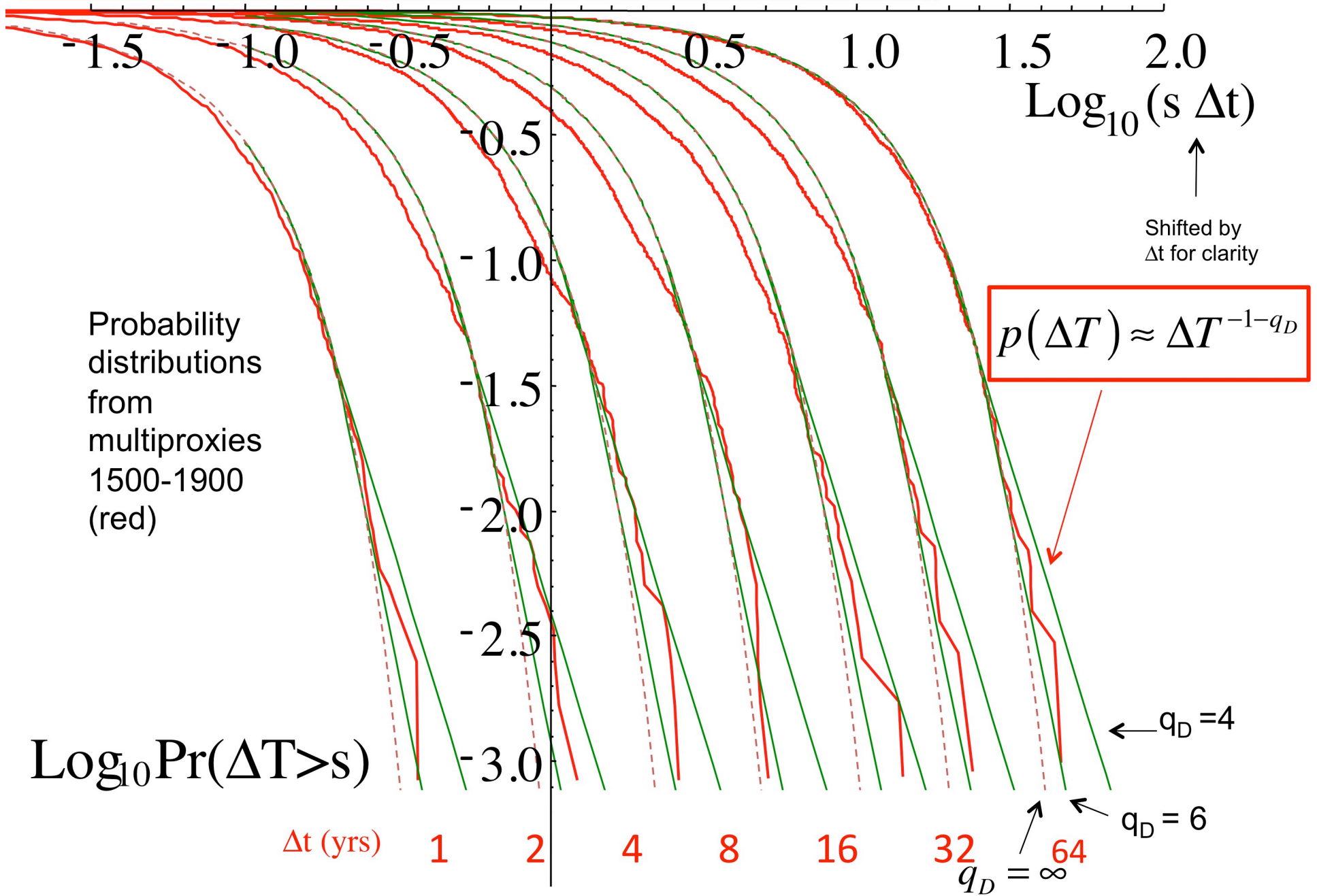
Statistical hypothesis testing

To be as rigorous and convincing as possible, we must demonstrate that the probability that the current warming is a natural fluctuation is low enough so that the natural variability hypothesis may be rejected with high levels of confidence.

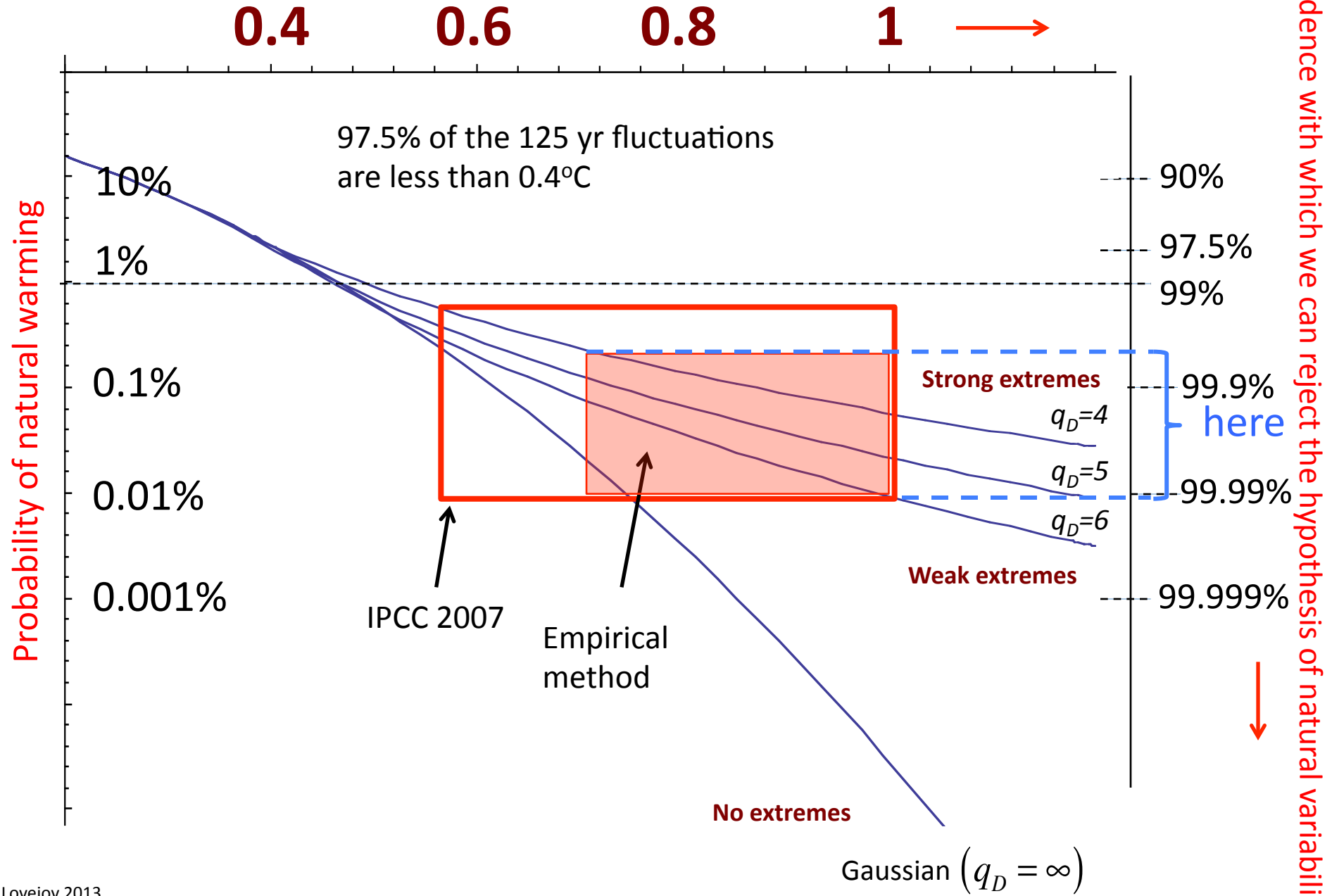
GCM's can't provide reliable centennial scale probabilities, *we need multiproxies.*

Bracketing the temperature extremes with power laws

$$s^{-4} > \Pr(\Delta T > s) > s^{-6}$$

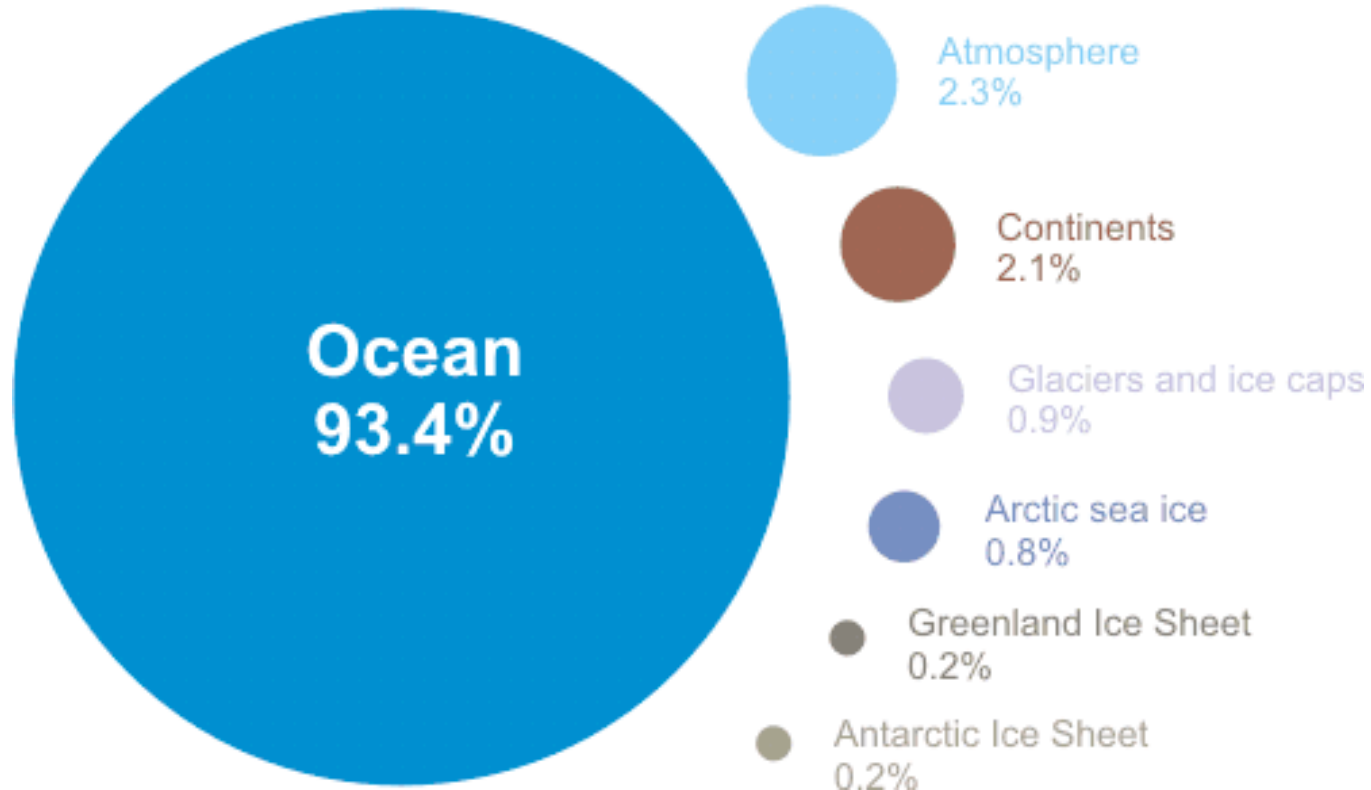


Anthropogenic Warming 1880-2004 (°C)

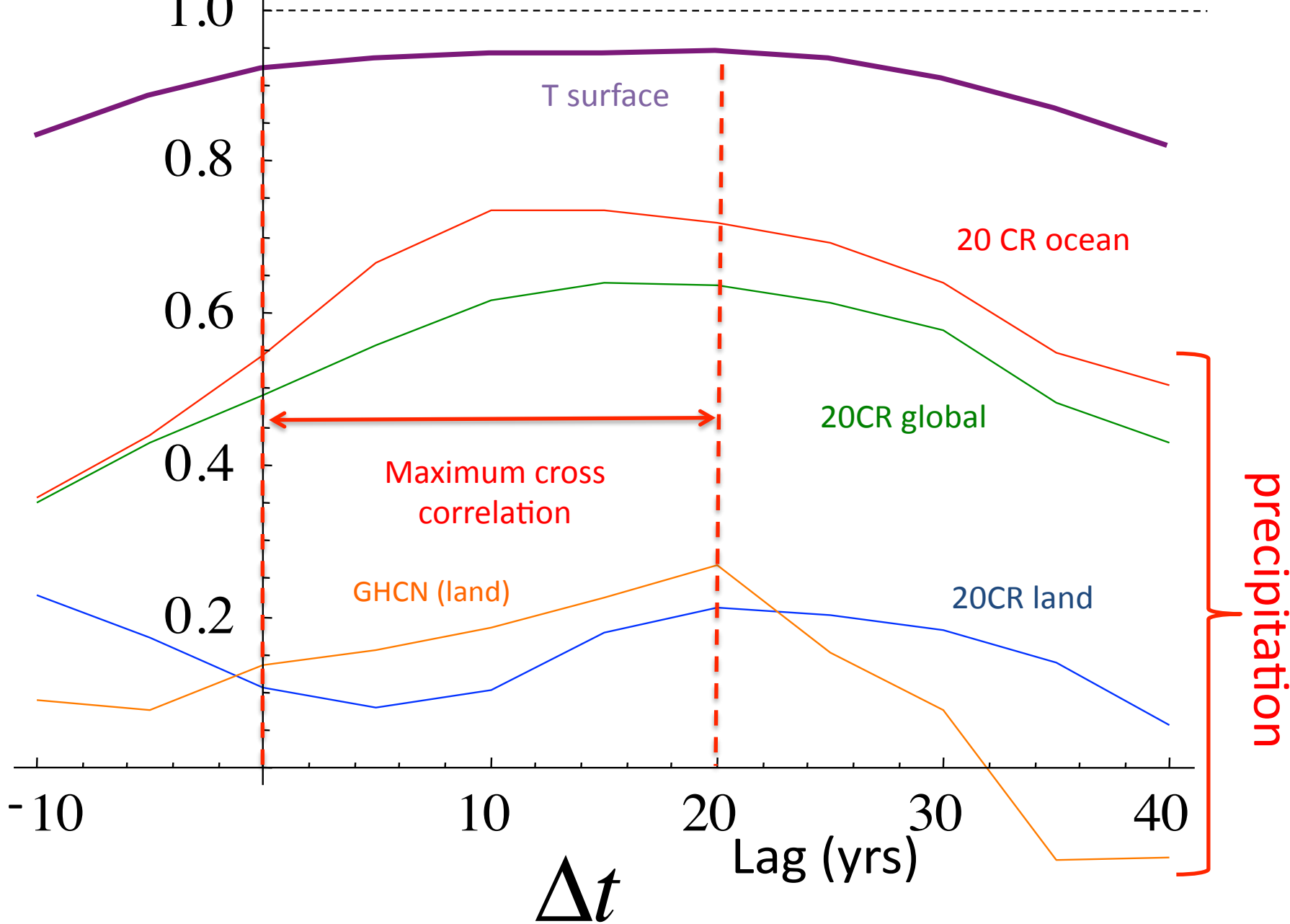


Ocean-Atmosphere Lag

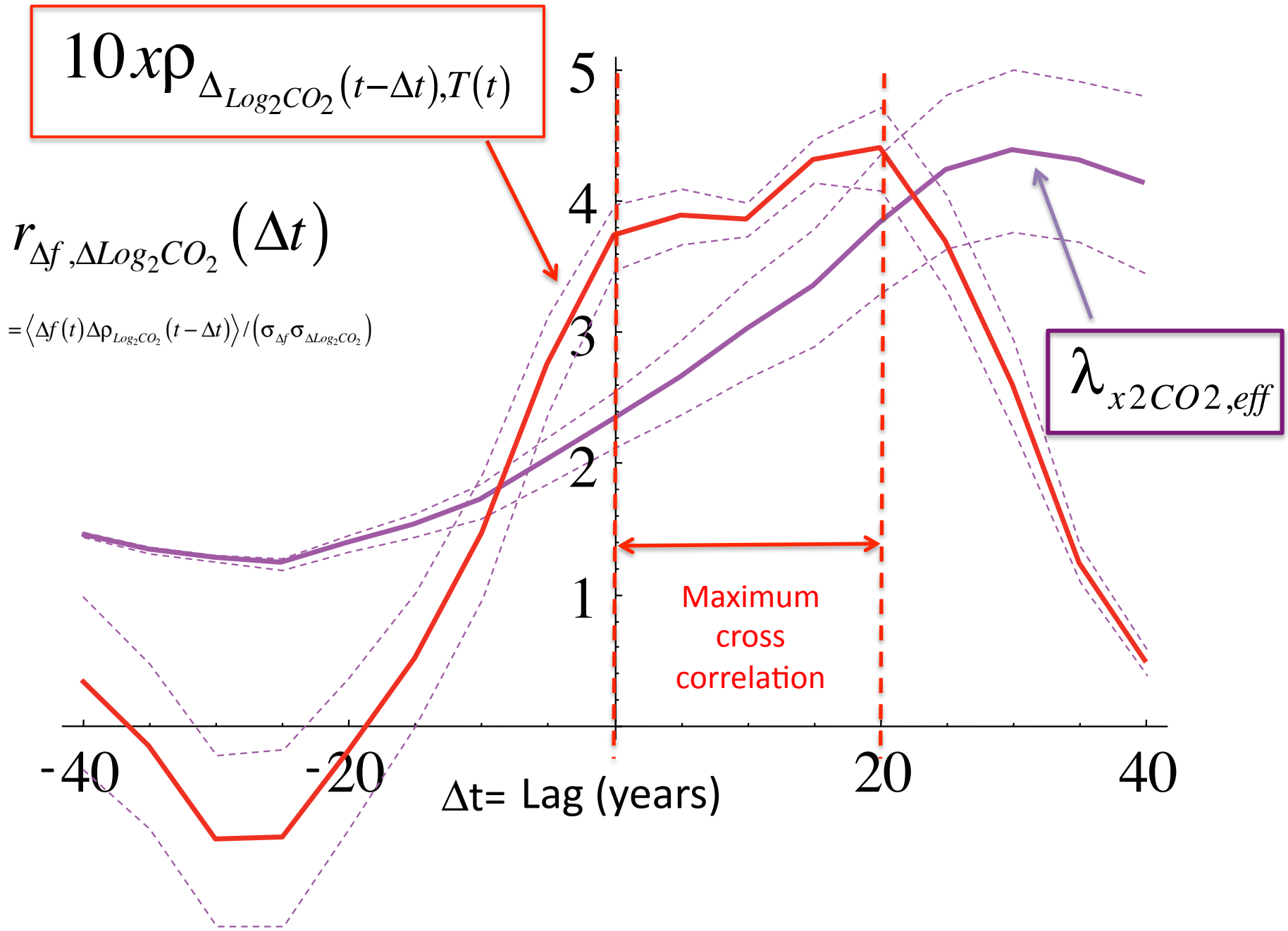
Most of the direct heating goes to the ocean:



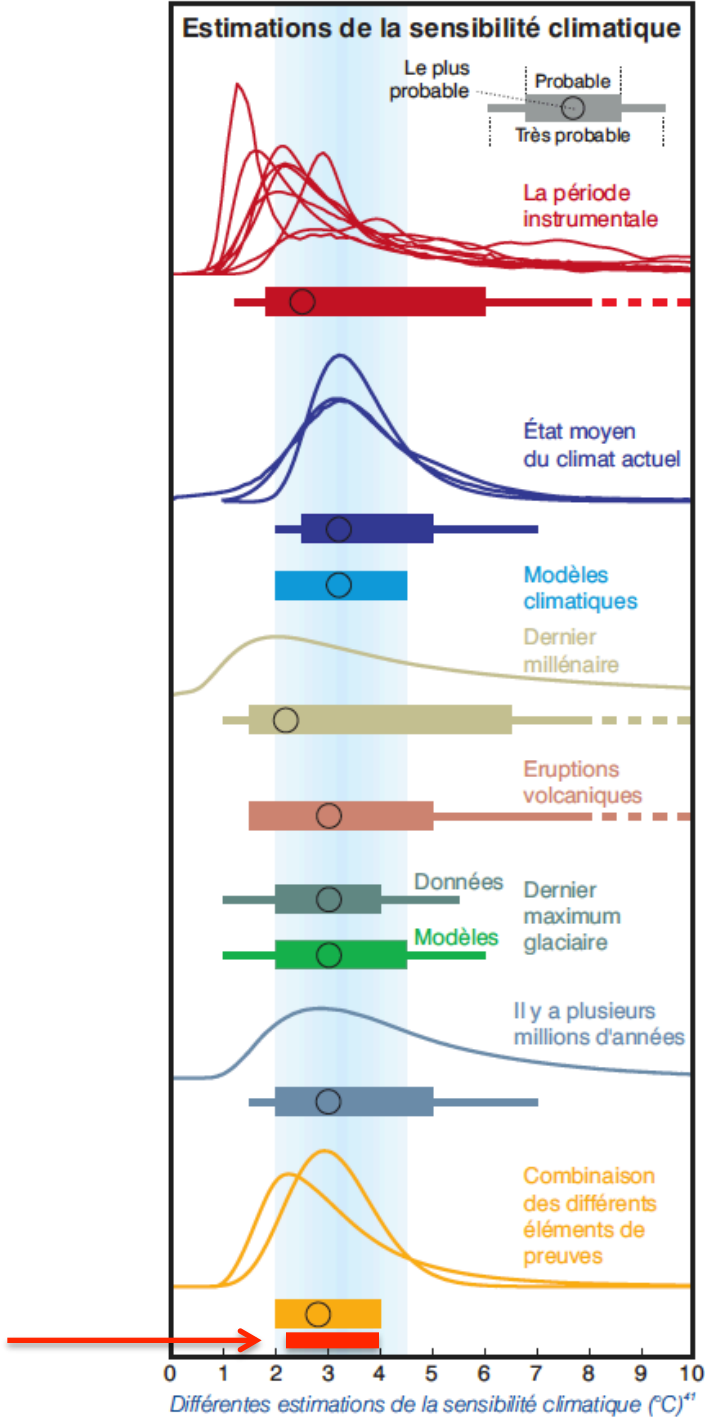
$$r_{f, \text{Log}_2 \text{CO}_2}(\Delta t) = \langle f(t) \rho_{\text{Log}_2 \text{CO}_2}(t - \Delta t) \rangle / (\sigma_f \sigma_{\text{Log}_2 \text{CO}_2}) \quad \text{Crosscorrelations}$$



Fluctuation crosscorrelations, effective climate sensitivities: 1880- 2004



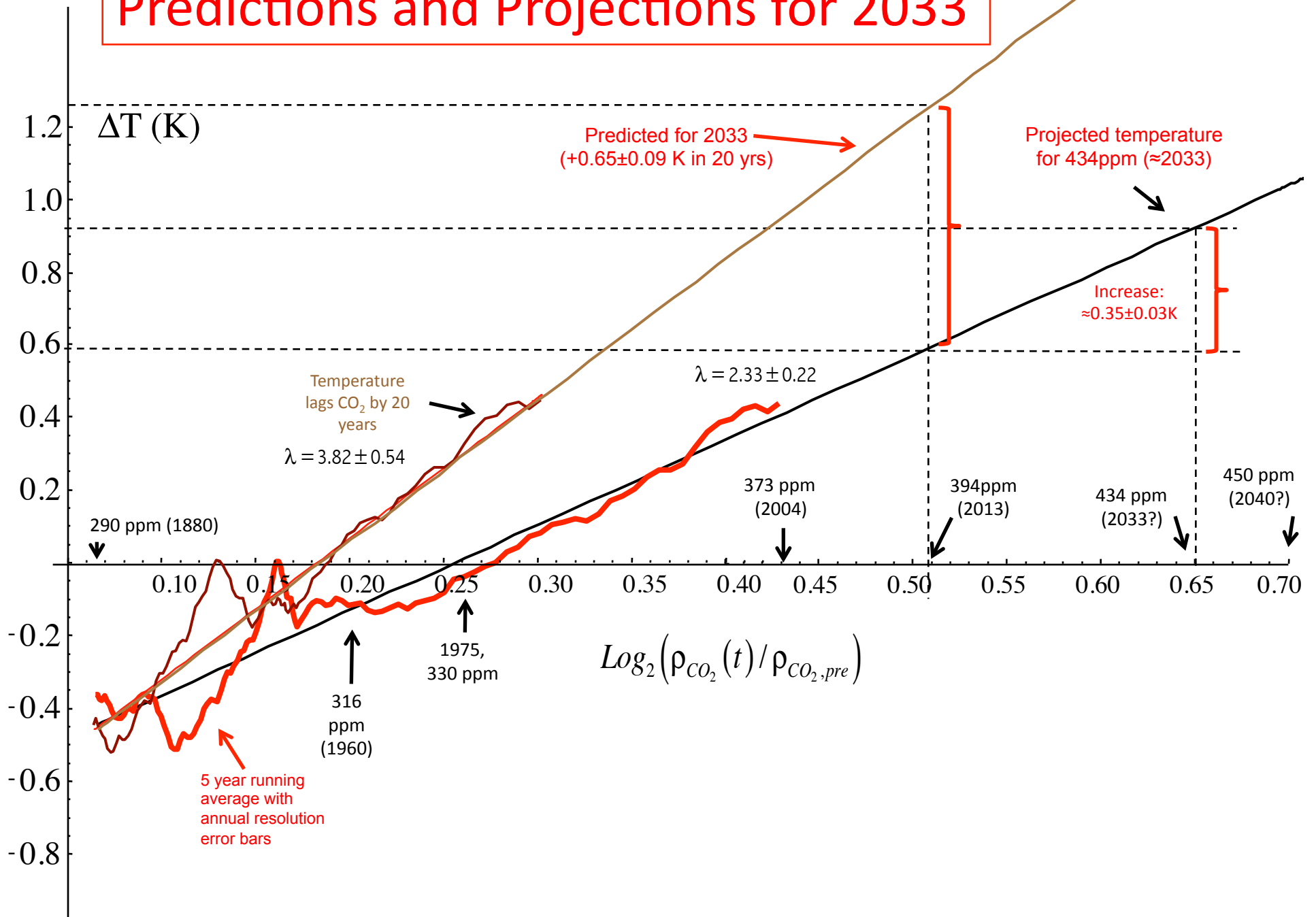
Various estimates of temperature increase with a doubling of CO₂



Our simple demonstration
3.08±0.58°C

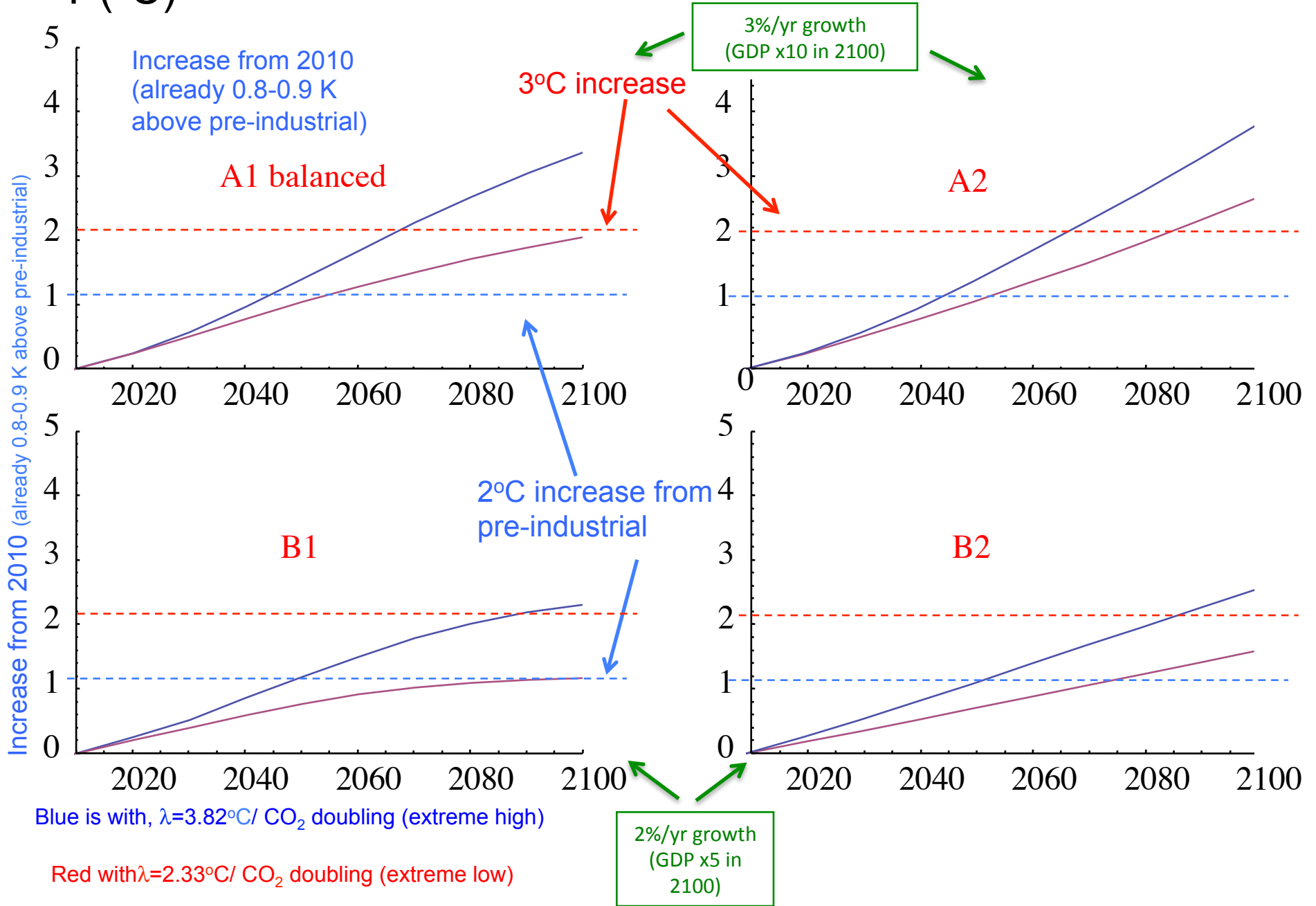
(Knutti et al 2008)

Predictions and Projections for 2033



SRES (Special Report on Emissions Scenarios, IPCC)

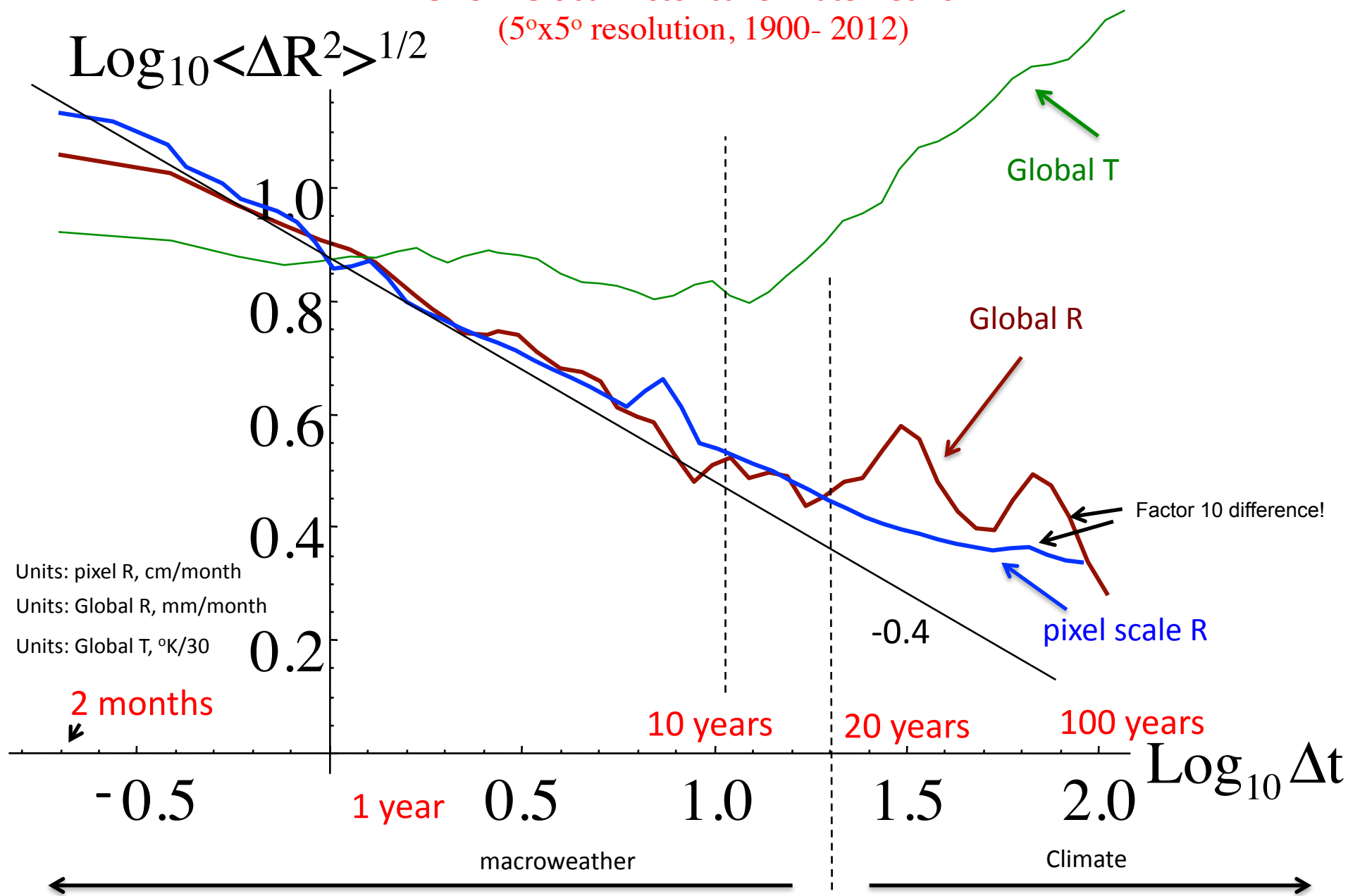
T (°C)

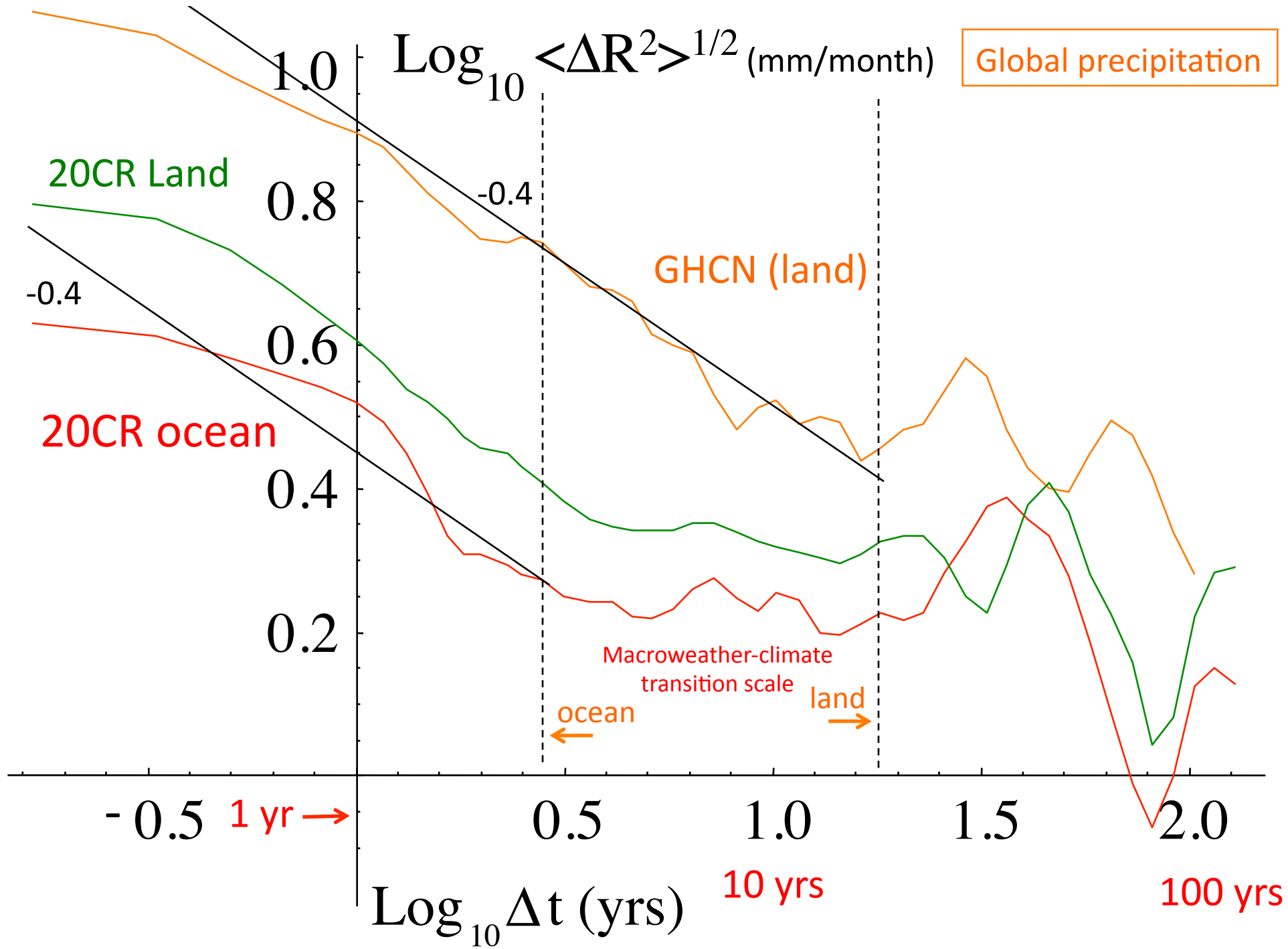


GCM-free analysis of Anthropogenic impacts on Precipitation

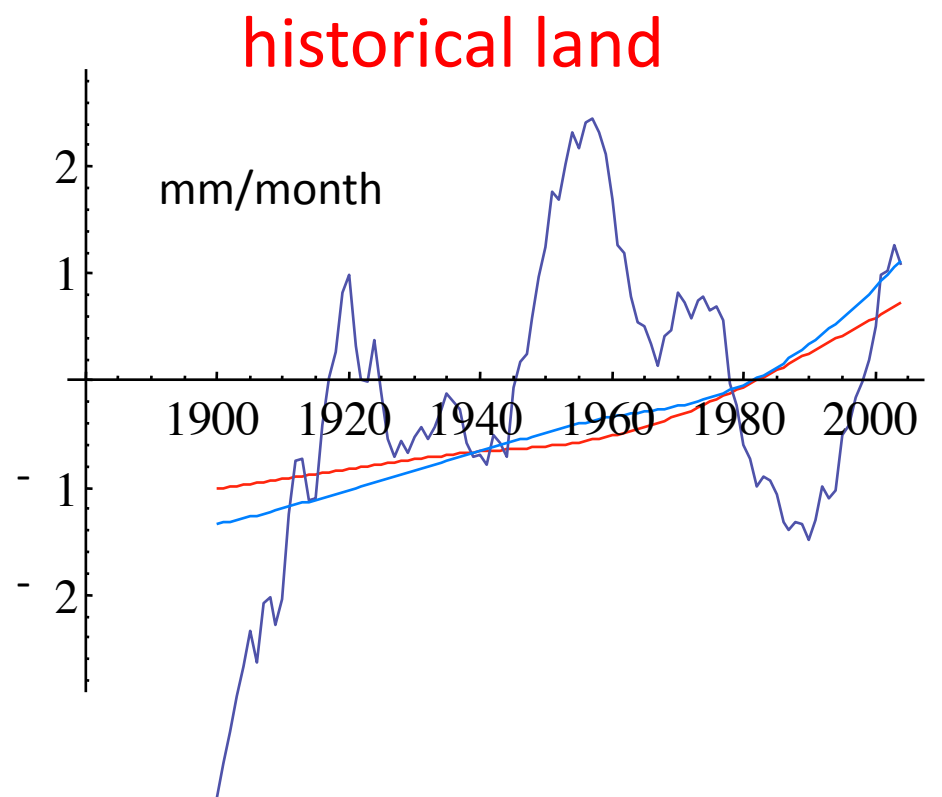
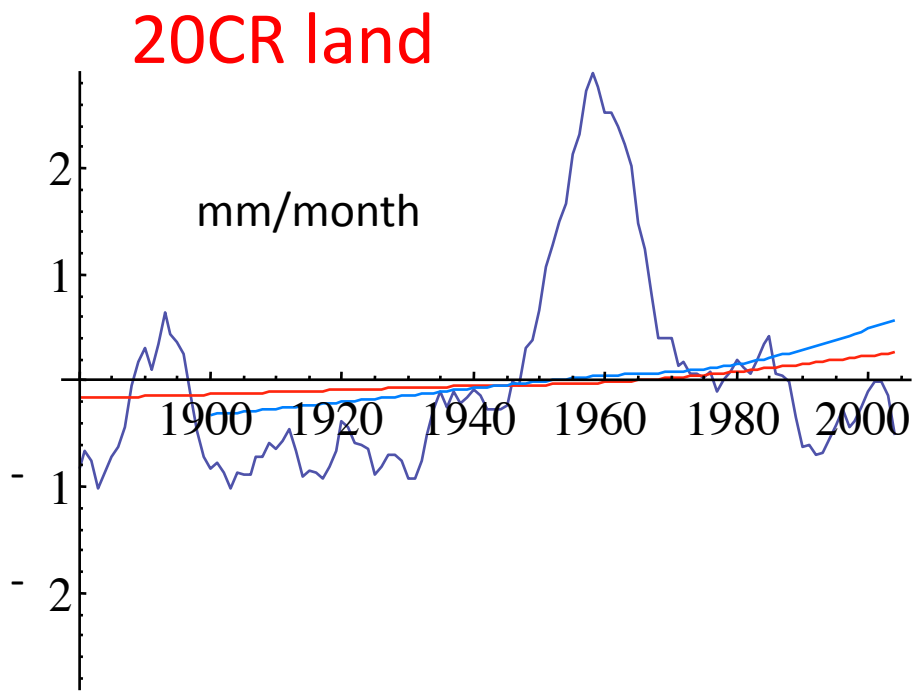
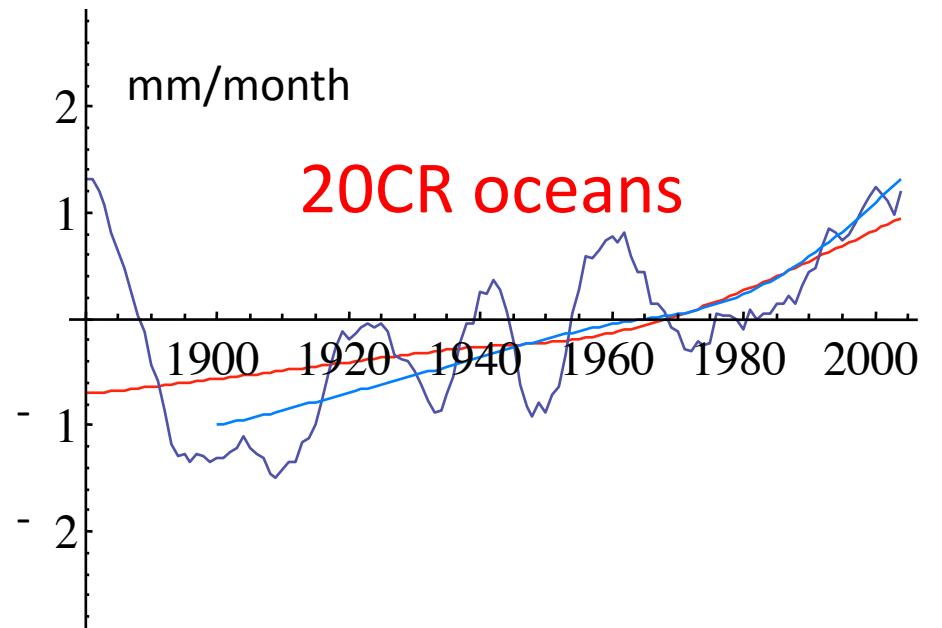
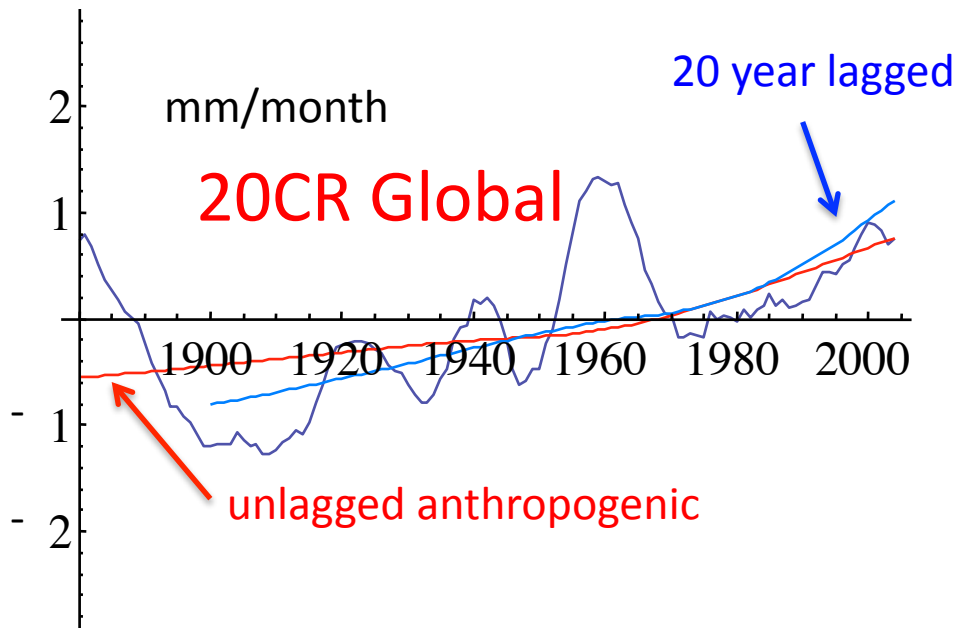
Precipitation and temperature:

GHCN=Global Historical Climate Network
(5°x5° resolution, 1900- 2012)

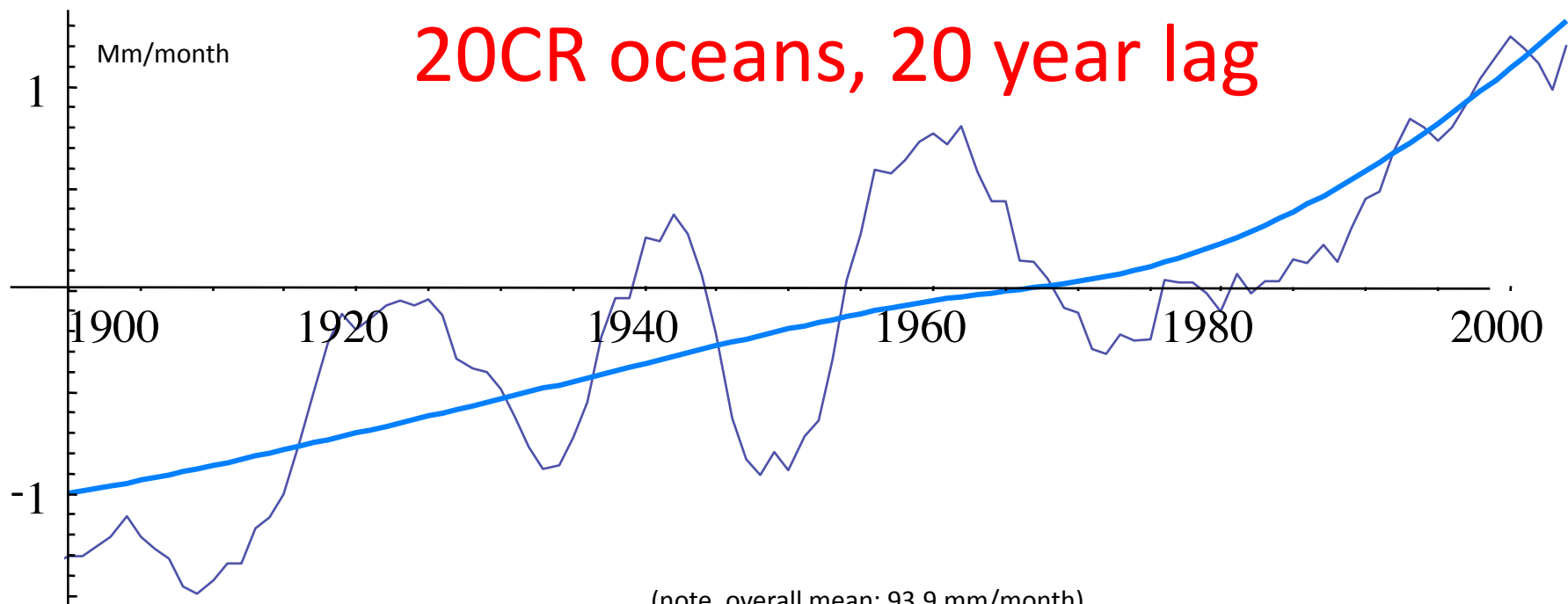




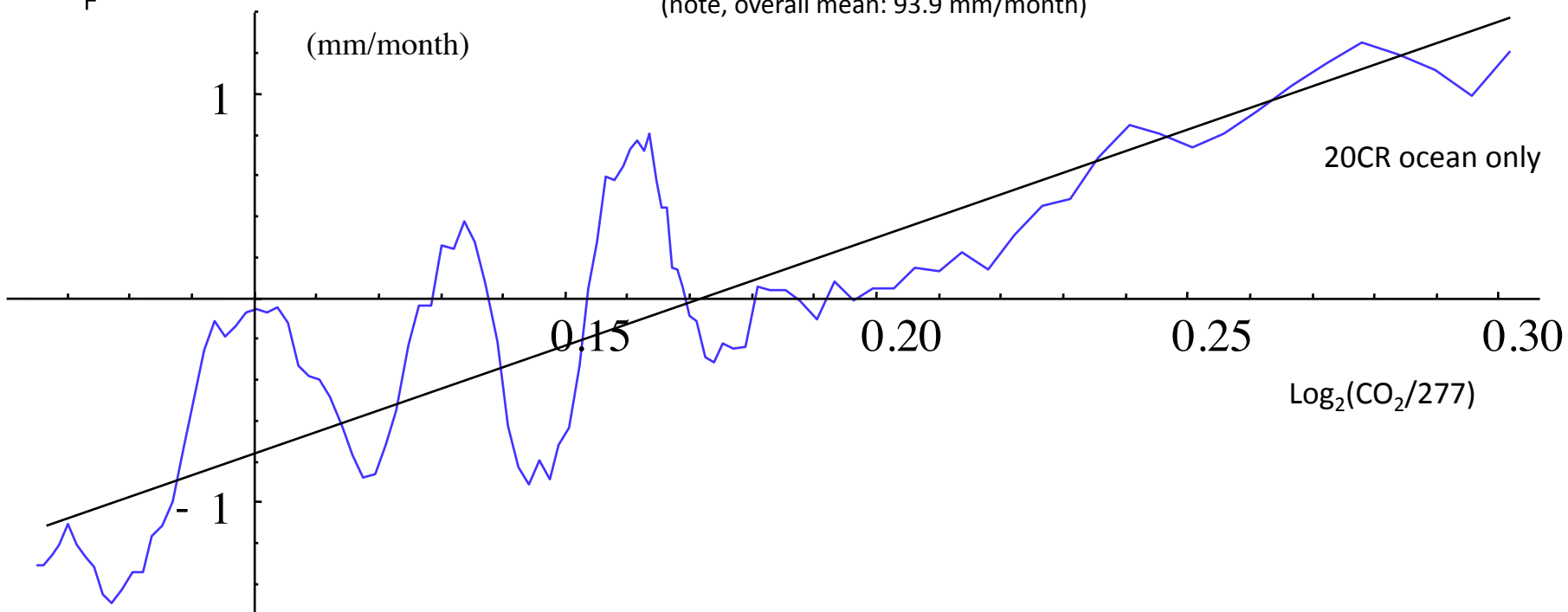
Quantifying Anthropogenic changes in precipitation



20CR oceans, 20 year lag



(note, overall mean: 93.9 mm/month)



Anthropogenic precipitation: increase rates for CO₂ doubling

	land	ocean	global
20CR, 0 lag	1.17±2.64	4.54±1.90	3.61±1.53
20CR, 20 yr lag	3.78±4.75	9.79±3.05	8.12±2.57
GHCN, 0 yr lag	5.18±3.64		
GHCN, 20 yr lag	10.37±5.43		

Red:
increasing trend
statistically
significant at
95% level

All in mm/month, values for CO₂ doubling.

error bars are one standard deviation estimates.

20CR= Twentieth Century reanalysis, GHCN=Global Historical Climate Network.

Ocean mean: 93.9221 mm/month
Land mean: 84.5933 mm/month,
Global: 91.33 mm/month

Decadal increases in precipitation rate comparison IPCC4

	land	ocean	global
20CR, 0 lag	0.45±1.00	1.73±0.72	1.37±0.58
20CR, 20 yr lag	1.44±1.81	3.73±1.16	3.09±0.98
GHCN, 0 yr lag	1.97±1.39		
GHCN, 20 yr lag	3.94±2.07		
CRU (from, IPCC4)	1.10±1.50		
GHCN (from, IPCC4)	1.08±1.87		

Red: statistically significant at 95% level

Blue: significant at 68% level

Green: not significant

IPCC4 (2007)

Above are inferred anthropogenic increases in precip over the period 1900-2005 in mm/year/decade (\log_2 CO₂/277 increased by 0.333 over this period).

IPCC estimates are from decadal scale linear regressions (not w.r.t. CO₂ forcing). Since macroweather continues to about 30 years for precipitation, these are not statistically significant.

Conclusions

1. Using scaling fluctuation analysis to characterizing the climate by its type of variability: expect macroweather not climate
2. The need for GCM-free approaches:
 - a) their climate not ours,
 - b) disarming climate skeptics
 - c) Using statistical hypothesis testing to rule out natural variability
3. Anthropogenic warming dominates macroweather at about 10 years rather than about 100 years (preindustrial).
4. The total anthropogenic warming is about 0.85°C , for CO_2 doubling, $3.08 \pm 0.58^{\circ}\text{C}$, GCM's: $1.5\text{-}4.5^{\circ}\text{C}$ (1979-2013).
5. The probability that the warming since 1880 is natural is $<1\%$ (most likely $<0.1\%$).
6. Precipitation is much "noisier" than temperature; anthropogenic effects detected mostly over ocean, not land, ≈ 30 year scale needed The total anthropogenic increase (oceans) is 9.79 ± 3.05 mm/month for CO_2 doubling ($>10\%$ increase: highly statistically significant).

